

The neldermead Package - version 1.0-8

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February 3, 2014

neldermead is a R port of a module originally developed for Scilab version 5.2.1 by Michael Baudin (INRIA - DIGITEO). Information about this software can be found at www.scilab.org. The following documentation as well as the content of the functions .Rd files are adaptations of the documentation provided with the original Scilab neldermead module.

neldermead currently does not include any adaptation of the Scilab 'nmplot' function series that is available in the original neldermead module.

1 Overview

1.1 Description

The goal of this toolbox is to provide several direct search optimization algorithms based on the simplex method. The optimization problem to solve is the minimization of a cost function, with bounds and nonlinear constraints.

$$\begin{aligned} & \min f(x) \\ & l_i \leq x_i \leq h_i, \quad i = 1, n \\ & g_j(x) \geq 0, \quad j = 0, nbineq \end{aligned}$$

where f is the cost function, x is the vector of parameter estimates, l and h are vectors of lower and upper bounds for the parameter estimates, n is the number of parameters and $nbineq$ the number of inequality constraints $g(x)$.

The provided algorithms are direct search algorithms, i.e. algorithms which do not use the derivative of the cost function. They are based on the update of a simplex, which is a set of $k \geq n + 1$ vertices, where each vertex is associated with one point and one function value.

The following algorithms are available:

- The fixed shape simplex method of Spendley, Hext and Hinsworth: this algorithm solves an unconstrained optimization problem with a fixed shape simplex made of $k = n + 1$ vertices.
- The variable shape simplex method of Nelder and Mead: this algorithm solves an unconstrained optimization problem with a variable shape simplex made of $k = n + 1$ vertices [3].
- Box's complex method: this algorithm solves an constrained optimization problem with a variable shape simplex made of an arbitrary k number of vertices ($k = 2n$ is recommended by Box).

1.2 Basic object

The basic object used by the **neldermead** package to store the configuration settings and the history of an optimization is a 'neldermead' object, i.e. a list typically created by **neldermead** and having a strictly defined structure (see `?neldermead` for more details).

1.3 The cost function

The **function** element of the neldermead object allows to configure the cost function. The cost function is used to compute the objective function value **f**. If the **nbineqconst** element of the neldermead object is configured to a non-zero value, the cost function must also compute the value of the nonlinear, positive, inequality constraints **c**. The cost function can also take as input/output an additional argument, if the **costfargument** element is configured. The function should be defined as described in `vignette('optimbase', package='optimbase')`:

```
costf <- function(x, index, fmsfodata){  
  # Define f and c here #  
  return(list(f, g=NULL, c, gc=NULL, index=index,  
             this=list(costfargument = fmsfodata)))  
}
```

where

- x**: is the current point, as a column vector,
- index**: (optional), an integer representing the value to compute, and
- fmsfodata**: an user-provided input/output argument.
- f**: the value of the objective function (a scalar),
- g**: typically the gradient of the objective function in the context of the **optimbase** functions; must be set to NULL as the Nelder-Mead is not gradient-based,
- c**: the vector of values of non-linear, positive, inequality constraints,
- gc**: typically the gradient of the constraints in the context of the **optimbase** functions; must be set to NULL as the Nelder-Mead is not gradient-based,
- this**: must be set to `list(costfargument = fmsfodata)`.

The index input parameter tells the cost function what to return as output arguments (as described in `vignette('optimbase', package='optimbase')`). It has the following meaning:

- index = 2**: compute **f**,
- index = 5**: compute **c**,
- index = 6**: compute **f** and **c**

The `fmsdata` argument is both input and output. This feature may be used in the situation where the cost function has to update its environment from call to call. Its simplest use is to count the number of calls to the cost function, but this feature is already available directly. Consider the more practical situation where the optimization requires the execution of an underlying Newton method (a chemical solver for example). This Newton method requires an initial guess x_0 . If the initial guess for this underlying Newton method is kept constant, the Newton method may have problems to converge when the current optimization point get far away from the its initial point. If a `costfargument` element is defined in the `neldermead` object, it can be passed to the cost function as the `fmsdata` argument. In this case, the initial guess for the Newton method can be updated so that it gets the value of the previous call. This way, the Newton method will have less problems to converge and the cost function evaluation may be faster.

We now present how the feature works. Everytime the cost function is called back, the `costfargument` element is passed to the cost function as an input argument. If the cost function modifies its content in the output argument, the content of the `costfargument` element is updated accordingly. Once the optimization is performed, the user may call the `neldermead.cget` function and get back an updated `costfargument` content.

1.4 The output function

The `outputcommand` element of the `neldermead` object allows to configure a command which is called back at the start of the optimization, at each iteration and at the end of the optimization. The output function must be defined as follows:

```
outputcmd <- function(state, data, myobj)
```

where

`state`: is a string representing the current state of the algorithm. Available values are 'init', 'iter', and 'done',

`data`: a list containing at least the following entries:

`x`: the current optimum,

`fval`: the current function value,

`iteration`: the current iteration index,

`funccount`: the number of function evaluations,

`simplex`: the current simplex,

`step`: the previous step in the algorithm. The following values are available: 'init', 'done', 'reflection', 'expansion', 'insidecontraction', 'outsidecontraction', 'reflectionnext', and 'shrink',

`myobj`: a user-defined parameter. This input parameter is defined with the `outputcommandarg` element of the `neldermead` object.

The output function may be used when debugging the specialized optimization algorithm, so that a verbose logging is produced. It may also be used to write one or several report files in a specialized format (ASCII, L^AT_EX, Excel, etc...). The user-defined parameter may be used in that case to store file names or logging options.

The `data` list argument may contain more fields than the current presented ones. These additionnal fields may contain values which are specific to the specialized algorithm, such as the simplex in a Nelder-Mead method, the gradient of the cost function in a BFGS method, etc...

1.5 Termination

The current package takes into account several generic termination criteria. The following termination criteria are enabled by default:

- maxiter,
- maxfunevals,
- tolxmethod,
- tolsimplexizemethod.

The `neldermead.termination` function uses a set of rules to compute if the termination occurs and sets optimization status to one of the following: 'continue', 'maxiter', 'maxfunevals', 'tolf', 'tolx', 'tolsize', 'tolsizedeltafv', 'kelleystagnation', 'tolboxf' or 'tolvariance'. The value of the status may also be a user-defined string, in the case where a user-defined termination function has been set.

The following set of rules is examined in this order.

- By default, the status is 'continue' and the terminate flag is FALSE.
- The number of iterations is examined and compared to the `maxiter` element of the `neldermead` object: if `iterations` \geq `maxiter`, then the status is set to 'maxiter' and terminate is set to TRUE.
- The number of function evaluations is examined and compared to the `maxfunevals` elements: if `funevals` \geq `maxfunevals`, then the status is set to 'maxfuneval' and terminate is set to TRUE.
- The tolerance on function value is examined depending on the value of the `tolfunmethod`.

FALSE: then the criteria is just ignored,

TRUE: if $|currentfopt| < tolfunrelative \cdot |previousfopt| + tolfunabsolute$, then the status is set to 'tolf' and terminate is set to TRUE.

The relative termination criteria on the function value works well if the function value at optimum is near zero. In that case, the function value at initial guess `fx0` may be used as `previousfopt`. This criteria is sensitive to the `tolfunrelative` and `tolfunabsolute` elements. The absolute termination criteria on the function value works if the user has an accurate idea of the optimum function value.

- The tolerance on x is examined depending on the value of the `tolxmethod` element.

FALSE: then the criteria is just ignored,

TRUE: if $\text{norm}(\text{currentxopt} - \text{previousxopt}) < tolxrelative \cdot \text{norm}(\text{currentxopt}) + tolxabsolute$, then the status is set to 'tolx' and terminate is set to TRUE.

This criteria is sensitive to the `tolxrelative` and `tolxabsolute` elements. The relative termination criteria on x works well if x at optimum is different from zero. In that case, the condition measures the distance between two iterates. The absolute termination criteria on x works if the user has an accurate idea of the scale of the optimum x. If the optimum x is near 0, the relative tolerance will not work and the absolute tolerance is more appropriate.

- The tolerance on simplex size is examined depending on the value of the `tolsimplexizemethod` element.
 FALSE: then the criteria is just ignored,
 TRUE: if $\text{ssize} < \text{tolsimplexizerelative} \cdot \text{simplexsize0} + \text{tolsimplexizeabsolute}$,
 where `simplexsize0` is the size of the simplex at iteration 0, then the status is set to
 'tolsize' and terminate is set to TRUE.
 The size of the simplex is computed from the 'sigmaplus' method of the **optimsimplex** package.
 This criteria is sensitive to the `tolsimplexizeabsolute` and the `tolsimplexizerelative` elements.
- The absolute tolerance on simplex size and absolute difference of function value is examined depending on the value of the `tolssizedeltafvmethod` element.
 FALSE: then the criteria is just ignored,
 TRUE: if both the following conditions $\text{ssize} < \text{tolsimplexizeabsolute}$ and $\text{shiftfv} < \text{toldelta}$
 are true where `ssize` is the current simplex size and `shiftfv` is the absolute value of the
 difference of function value between the highest and lowest vertices, then the status is set
 to 'tolssizedeltafv' and terminate is set to TRUE.
- The stagnation condition based on Kelley sufficient decrease condition is examined depending on the value of the `kelleystagnationflag` element.
 FALSE: then the criteria is just ignored,
 TRUE: if $\text{newfvmean} \leq \text{oldfvmean} - \alpha \cdot t(\text{sg}) \cdot \text{sg}$ where `newfvmean` (resp. `oldfvmean`)
 is the function value average in the current iteration (resp. in the previous iteration), then
 the status is set to 'kelleystagnation' and terminate is set to TRUE. Here, `alpha` is a non-
 dimensional coefficient and `sg` is the simplex gradient.
- The termination condition suggested by Box is examined depending on the value of the `boxtermination` element.
 FALSE: then the criteria is just ignored,
 TRUE: if both the following conditions $\text{shiftfv} < \text{boxtolf}$ and $\text{boxkount} == \text{boxnbmatch}$
 are true, where `shiftfv` is the difference of function value between the best and worst
 vertices, and `boxkount` is the number of consecutive iterations where this criteria is met,
 then the status is set to 'tolboxf' and terminate is set to TRUE. Here, the `boxtolf`
 parameter is the value associated with the `boxtolf` element of the `neldermead` object and
 is a user-defined absolute tolerance on the function value. The `boxnbmatch` parameter
 is the value associated with the `boxnbmatch` element and is the user-defined number of
 consecutive match.
- The termination condition based on the variance of the function values in the simplex is examined depending on the value of the `tolvarianceflag` element.
 FALSE: then the criteria is just ignored,
 TRUE: if $\text{var} < \text{tolrelativevariance} \cdot \text{variancesimplex0} + \text{tolabsolutevariance}$, where
 `var` is the variance of the function values in the simplex, then the status is set to
 'tolvariance' and terminate is set to TRUE. Here, the `tolrelativevariance` parameter
 is the value associated with the `tolrelativevariance` element of the `neldermead`

object and is a user-defined relative tolerance on the variance of the function values. The `tolabsolutevariance` parameter is the value associated with the `tolabsolutevariance` element and is the user-defined absolute tolerance of the variance of the function values.

- The user-defined termination condition is examined depending on the value of the `myterminateflag` element.

FALSE: then the criteria is just ignored,

TRUE: if the `term` boolean output argument returned by the termination function is TRUE, then the status is set to the user-defined status and terminate is set to TRUE.

1.6 Kelley's stagnation detection

The stagnation detection criteria suggested by Kelley is based on a sufficient decrease condition, which requires a parameter $\alpha > 0$ to be defined [1]. The `kelleynormalizationflag` element of the `neldermead` object allows to configure the method to use to compute this α parameter. Two methods are available, where each method corresponds to a different paper by Kelley:

constant: in 'Detection and Remediation of Stagnation in the Nelder-Mead Algorithm Using a Sufficient Decrease Condition', Kelley uses a constant α , with the suggested value 1.e-4, which is the typical choice for line search method.

normalized: in 'Iterative Methods for Optimization', Kelley uses a normalized α , computed from the following formula: $\alpha = \alpha_0 \cdot \sigma_0 / nsg$, where σ_0 is the size of the initial simplex and nsg is the norm of the simplex gradient for the initial guess point.

1.7 O'Neill's factorial optimality test

In 'Algorithm AS47 - Function minimization using a simplex procedure', O'Neill presents a fortran 77 implementation of the simplex method [5]. A factorial test is used to check if the computed optimum point is a local minimum. If the `restartdetection` element of the `neldermead` object is set to 'oneill', that factorial test is used to see if a restart should be performed.

1.8 Implementation notes of the method of Spendley *et al.*

The original paper may be implemented with several variations, which might lead to different results [6]. This section defines what algorithmic choices have been used in the present package.

The paper states the following rules.

- 'Rule 1. Ascertain the lowest reading y_i of $y_1 \dots y_{k+1}$. Complete a new simplex S_p by excluding the point V_p corresponding to y_i , and replacing it by V^* defined as above.'
- 'Rule 2. If a result has occurred in $(k + 1)$ successive simplexes, and is not then eliminated by application of Rule 1, do not move in the direction indicated by Rule 1, or at all, but discard the result and replace it by a new observation at the same point.'
- 'Rule 3. If y is the lowest reading in S_o , and if the next observation made, y^* , is the lowest reading in the new simplex S_p , do not apply Rule 1 and return to S_o from S_p . Move out of S_o by rejecting the second lowest reading (which is also the second lowest reading in S_o).'

We implement the following 'rules' of the Spendley *et al.* method:

- Rule 1 is strictly applied, but the reflection is done by reflection of the high point, since we minimize a function instead of maximizing it, like Spendley.
- Rule 2 is NOT implemented, as we expect that the function evaluation is not subject to errors.
- Rule 3 is applied, i.e. reflection with respect to next to the high point. The original paper does not mention any shrink step. When the original algorithm cannot improve the function value with reflection steps, the basic algorithm stops. In order to make the current implementation of practical value, a shrink step is included, with shrinkage factor sigma. This perfectly fits into the spirit of the original paper. Notice that the shrink step makes the rule #3 (reflection with respect to next-to-worst vertex) unnecessary. Indeed, the minimum required steps are the reflection and shrinkage. Nevertheless, the rule #3 has been kept in order to make the algorithm as close as it can be to the original.

1.9 Implementation notes on the method of Nelder and Mead

The purpose of this section is to analyse the current implementation of Nelder-Mead's algorithm. The algorithm that we use is described in 'Iterative Methods for Optimization' by Kelley.

The original paper uses a 'greedy' expansion, in which the expansion point is accepted whatever its function value. The current implementation, as most implementations, uses the expansion point only if it improves over the reflection point, that is,

- if $f_e < f_r$, then the expansion point is accepted,
- if not, the reflection point is accepted.

The termination criteria suggested by Nelder and Mead is based on an absolute tolerance on the standard deviation of the function values in the simplex. We provide this original termination criteria with the `tolvarianceflag` element of the `neldermead` object, which is disabled by default.

1.10 Box's complex algorithm implementation notes

In this section, we analyse the current implementation of Box's complex method [4]. The initial simplex can be computed as in Box's paper, but this may not be safe. In his paper, Box suggests that if a vertex of the initial simplex does not satisfy the non linear constraints, then it should be 'moved halfway toward the centroid of those points already selected'. This behaviour is available when the `scalingsimplex0` element of the `neldermead` object is set to 'tocenter'. It may happen, as suggested by Guin [2], that the centroid is not feasible if the constraints are not convex. In this case, the initial simplex cannot be computed. This is why we provide the 'tox0' option, which allows to compute the initial simplex by scaling toward the initial guess, which is always feasible.

In Box's paper, the scaling into the non linear constraints is performed 'toward' the centroid, that is, by using a scaling factor equal to 0.5. This default scaling factor might be sub-optimal in certain situations. This is why we provide the `boxineqscaling` element, which allows to configure the scaling factor.

In Box's paper, whether we are concerned with the initial simplex or with the simplex at a given iteration, the scaling for the non linear constraints is performed without end. This is because Box's hypothesis is that 'ultimately, a satisfactory point will be found'. As suggested by Guin, if the process fails, the algorithm goes into an infinite loop. In order to avoid this, we perform the scaling until a minimum scaling value is reached, as defined by the `guinalphamin` element.

We have taken into account the comments by Guin, but it should be emphasized that the current implementation is still as close as possible to Box's algorithm and is not Guin's algorithm. More

precisely, during the iterations, the scaling for the non linear constraints is still performed toward the centroid, be it feasible or not.

1.11 User-defined algorithm

The `mymethod` element of the `neldemead` object allows to configure a user-defined simplex-based algorithm. The reason for this option is that many simplex-based variants of Nelder-Mead's algorithm have been developped over the years, with specific goals. While it is not possible to provide them all, it is very convenient to use the current structure without being forced to make many developments.

The value of the `mymethod` element is expected to be a R function with the following structure:

```
> myalgorithm <- function( this ){
+   ...
+   return(this)
+ }
```

where `this` is the current `neldermead` object.

In order to use the user-defined algorithm, the `method` element must be set to 'mine'. In this case, the component performs the optimization exactly as if the user-defined algorithm was provided by the component.

The user interested in that feature may use the internal scripts provided in the distribution as templates and tune his own algorithm from that point. There is of course no warranty that the user-defined algorithm improves on the standard algorithm, so that users use this feature at their own risks.

1.12 User-defined termination

Many termination criteria are found in the literature. Users who aim at reproducing the results exhibited in a particular paper may find that that none of the provided termination criteria match the one which is used in the paper. It may also happen that the provided termination criteria are not suitable for the specific test case. In those situation the `myterminate` element of the `neldermead` object allows to configure a user-defined termination function. The value of the `myterminate` element is expected to be a R function with the following structure:

```
> mystoppingrule <- function( this , simplex ){
+   ...
+   return(list(this=this,terminate=terminate,status=status))
+ }
```

where `this` is the current `neldermead` object and `simplex` is the current simplex. The `terminate` output argument is a logical flag which is FALSE if the algorithm must continue and TRUE if the algorithm must stop. The `status` output argument is a string which is associated with the current termination criteria.

In order to enable the use of the user-defined termination function, the value of the `myterminateflag` element must be set to TRUE in the `neldermead` object. At each iteration, if the `myterminateflag` element has been set to TRUE, the user-defined termination is called. If the `terminate` output argument is TRUE, then the algorithm is stopped. In that case, the value of the `status` element of the `neldermead.get` function output is the value of the `status` output argument of the user-defined termination function.

2 Specialized functions

2.1 fminsearch

The `fminsearch` function is based on a specialized use of the more general `neldermead` function bundle and searches for the unconstrained minimum of a given cost function. This function corresponds to the Matlab (or Scilab) `fminsearch` function. In the context of `fminsearch`, the function to be minimized is not a cost function as described in Section 1.3 but an objective function (returning a numeric scalar). Additional information and examples are available in `?fminsearch` from a R environment.

2.2 Direct grid search

Direct grid search, performed by `fmin.gridsearch`, is a functionality added to the original Scilab `neldermead` module and constitutes another specialized use of the `neldermead` package. This function allows to explore the search space of an optimization problem around the initial point x_0 . This optimization problem is defined by an objective function, like for `fminsearch`, and not a cost function. `fmin.gridsearch` automatically creates a grid of search points selected around the initial point and evaluates the objective function at each point. The boundaries of the grid are set either by a vector of parameter-specific lower and upper limits, or by a vector of factors α as follows: $[x_0/\alpha, x_0 \times \alpha]$. The number $npts$ of points evaluated for each parameter (or dimension of the optimization problem) can also be defined. The total number of points in the grid is therefore $npts^n$. At the end of the search, `fmin.gridsearch` returns a table sorted by value of the objective function. The feasibility of the objective function is also determined at each point, as `fmin.gridsearch` is a wrapper around `optimbase.gridsearch` which assesses the feasibility of a cost function in addition to calculating its value at each particular search point. Because `fmin.gridsearch` does not accept constraints, the objective function should always be feasible. Additional information is available in `?fmin.gridsearch` from a R environment.

3 Examples

We present in this section basic examples illustrating the use of `neldermead` functions to optimize unconstrained or constrained systems. More complex examples are described in a Scilab-based document written by Michael Baudin and available at <http://forge.scilab.org/index.php/p/docneldermead/>. Because the R port of the Scilab `neldermead` module is almost literal, the user should be able to reproduce the described examples in R with minimal adaptations.

3.1 Example 1: Basic use

In the following example, we solve a simple quadratic test case. We begin by defining the cost function, which takes 3 input arguments and returns the value of the objective function as the `f` element of a list. The standard starting point $[-1.2 \ 1.0]$ is used. `neldermead` creates a new `neldermead` object. Then we use `neldermead.configure` to configure the parameters of the problem. We use all default settings and perform the search for the optimum. `neldermead.get` is finally used to retrieve the optimum parameters.

```
> quadratic <- function(x=NULL, index=NULL, fmsfunda=NULL){  
+   return(list(f=x[1]^2 + x[2]^2,  
+             g=c(),
```

```

+
+           c=c(),
+           gc=c(),
+           index=index,
+           this=list(costfargument=fmsfadata)))
+
+      }
> x0 <- transpose( c(1.0,1.0) )
> nm <- neldermead()
> nm <- neldermead.configure(nm, '-numberofvariables',2)
> nm <- neldermead.configure(nm, '-function',quadratic)
> nm <- neldermead.configure(nm, '-x0',x0)
> nm <- neldermead.search(nm)
> summary(nm)

Number of Estimated Variable(s): 2

Estimated Variable(s):
  Initial       Final
1     1 -1.010582e-08
2     1 -1.768891e-07

Cost Function:
function(x=NULL, index=NULL, fmsfadata=NULL){
  return(list(f=x[1]^2 + x[2]^2,
              g=c(),
              c=c(),
              gc=c(),
              index=index,
              this=list(costfargument=fmsfadata)))
}

Cost Function Argument(s):
[1] ""

Optimization:
- Status: "maxfuneval"
- Initial Cost Function Value: 2.000000
- Final Cost Function Value: 0.000000
- Number of Iterations (max): 52 (100)
- Number of Function Evaluations (max): 100 (100)

Simplex Information:

- Simplex at Initial Point:
Dimension: n=2
Number of vertices: nbve=3
  Vertex #1/3 : fv=2.000000e+00, x=1.000000e+00 1.000000e+00
  Vertex #2/3 : fv=5.000000e+00, x=2.000000e+00 1.000000e+00
  Vertex #3/3 : fv=5.000000e+00, x=1.000000e+00 2.000000e+00

```

```

- Simplex at Optimal Point:
Dimension: n=2
Number of vertices: nbve=3
  Vertex #1/3 : fv=3.139189e-14, x=-1.010582e-08 -1.768891e-07
  Vertex #2/3 : fv=1.290894e-13, x=-3.557479e-07 5.032676e-08
  Vertex #3/3 : fv=1.601186e-13, x=2.637847e-07 3.008924e-07

```

3.2 Example 2: Customized use

In the following example, we solve the Rosenbrock test case. We begin by defining the Rosenbrock function, which takes 3 input arguments and returns the value of the objective function. The standard starting point [-1.2 1.0] is used. `neldermead` creates a new `neldermead` object. Then we use `neldermead.configure` to configure the parameters of the problem. The initial simplex is computed from the axes and the single length 1.0 (this is the default, but is explicitly written here as an example). The variable simplex algorithm by Nelder and Mead is used, which corresponds to the -method 'variable' option. `neldermead.search` performs the search for the minimum. Once the minimum is found, we represent part of the search space using the `contour` function (this is possible since our problem involves only 2 parameters) and we superimpose the starting point (in red), the optimisation path (in blue), and the optimum (in green) to the plot. The history of the optimisation can be retrieved (using `neldermead.get`) because the '-storehistory' option was set to TRUE.

```

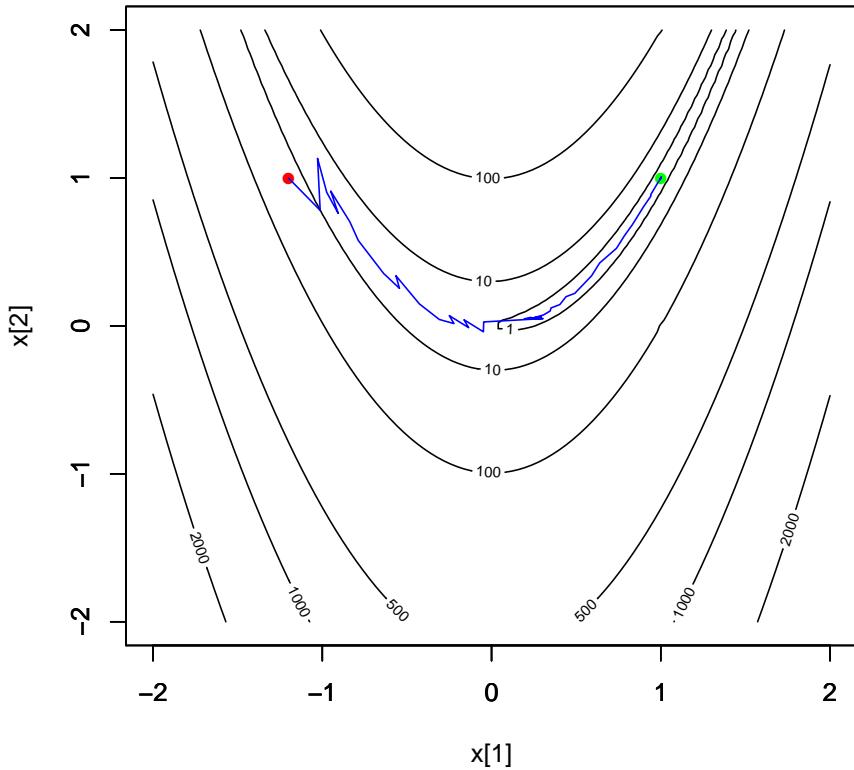
> rosenbrock <- function(x=NULL,index=NULL,fmsfodata=NULL){
+   return(list(f=100*(x[2]-x[1]^2)^2+(1-x[1])^2,
+             g=c(),
+             c=c(),
+             gc=c(),
+             index=index,
+             this=list(costfargument=fmsfodata)))
+ }
> x0 <- transpose(c(-1.2,1.0))
> nm <- neldermead()
> nm <- neldermead.configure(nm,'-numberofvariables',2)
> nm <- neldermead.configure(nm,'-function',rosenbrock)
> nm <- neldermead.configure(nm,'-x0',x0)
> nm <- neldermead.configure(nm,'-maxiter',200)
> nm <- neldermead.configure(nm,'-maxfunevals',300)
> nm <- neldermead.configure(nm,'-tolfunrelative',10*.Machine$double.eps)
> nm <- neldermead.configure(nm,'-tolxrelative',10*.Machine$double.eps)
> nm <- neldermead.configure(nm,'-simplex0method','axes')
> nm <- neldermead.configure(nm,'-simplex0length',1.0)
> nm <- neldermead.configure(nm,'-method','variable')
> nm <- neldermead.configure(nm,'-verbose',FALSE)
> nm <- neldermead.configure(nm,'-storehistory',TRUE)
> nm <- neldermead.configure(nm,'-verbosetermination',FALSE)
> nm <- neldermead.search(nm)
> xmin <- ymin <- -2.0
> xmax <- ymax <- 2.0
> nx <- ny <- 100
> stepy <- stepx <- (xmax - xmin)/nx

```

```

> ydata <- xdata <- seq(xmin,xmax,stepx)
> zdata <- apply(expand.grid(xdata,ydata),1,
+                     function(x) neldermead.function(nm,transpose(x)))
> zdata <- matrix(zdata,ncol=length(ydata))
> optimpath <- matrix(unlist((neldermead.get(nm, '-historyxopt'))),
+                     nrow=2)
> optimpath <- data.frame(x=optimpath[1,],y=optimpath[2,])
> contour(xdata,ydata,zdata,levels=c(1,10,100,500,1000,2000))
> par(new=TRUE,ann=TRUE)
> plot(c(x0[1],optimpath$x[158]), c(x0[2],optimpath$y[158]),
+       col=c('red','green'),pch=16,xlab='x[1]',ylab='x[2]',
+       xlim=c(xmin,xmax),ylim=c(ymin,ymax))
> par(new=TRUE,ann=FALSE)
> plot(optimpath$x,optimpath$y,col='blue',type='l',
+       xlim=c(xmin,xmax),ylim=c(ymin,ymax))

```



Setting the '-verbose' element of the neldermead object to 1 allows to get detailed information about the current optimization process. The following is a sample output for an optimization based on the Nelder and Mead variable-shape simplex algorithm. Only the output corresponding to the iteration #156 is displayed. In order to display specific outputs (or to create specific output files

and graphics), the '-outputcommand' option should be used.

```
=====
Iteration #156 (total = 156)
Function Eval #298
Xopt: 0.99999999999991 0.99999999999816
Fopt: 8.997809e-27
DeltaFv: 4.492261e-26
Center: 1.00000000000003 1.00000000000007
Size: 4.814034e-13
Vertex #2/3 : fv=2.649074e-26, x=1.000000e+00 1.000000e+00
Vertex #3/3 : fv=5.392042e-26, x=1.000000e+00 1.000000e+00
Reflect
xbar=1.00000000000001 1.00000000000003
Function Evaluation #299 at [0.9999999999996 ]
Function Evaluation #299 at [0.9999999999907 ]
xr=[0.9999999999996 0.9999999999907], f(xr)=0.000000
  > Perform reflection
Sort
```

3.3 Example 3: Optimization with bound constraints

In the following example, we solve a simple quadratic test case used in Example 1 but in the case where bounds are set for parameter estimates. We begin by defining the cost function, which takes 3 input arguments and returns the value of the objective function as the `f` element of a list. The starting point [1.2 1.9] is used. `neldermead` creates a new `neldermead` object. Then we use `neldermead.configure` to configure the parameters of the problem including the lower `-boundsmin` and upper `-boundsmax` bounds. The initial simplex is computed from `boxnbpoints` random points within the bounds. The variable simplex algorithm by Box is used, which corresponds to the `-method` 'box' option. `neldermead.search` finally performs the search for the minimum.

```
> quadratic <- function(x=NULL, index=NULL, fmsfndata=NULL) {
+   return(list(f=x[1]^2 + x[2]^2,
+             g=c(),
+             c=c(),
+             gc=c(),
+             index=index,
+             this=list(costfargument=fmsfndata)))
+ }
> set.seed(0)
> x0 <- transpose(c(1.2,1.9))
> nm <- neldermead()
> nm <- neldermead.configure(nm, '-numberofvariables',2)
> nm <- neldermead.configure(nm, '-function',quadratic)
> nm <- neldermead.configure(nm, '-x0',x0)
> nm <- neldermead.configure(nm, '-verbose',FALSE)
> nm <- neldermead.configure(nm, '-storehistory',TRUE)
> nm <- neldermead.configure(nm, '-verbosetermination',FALSE)
> nm <- neldermead.configure(nm, '-method','box')
```

```

>   nm <- neldermead.configure(nm, '-boundsmin', c(1,1))
>   nm <- neldermead.configure(nm, '-boundsmax', c(2,2))
>   nm <- neldermead.search(nm)
>   summary(nm)

Number of Estimated Variable(s): 2

Estimated Variable(s):
  Initial    Final Lower bound Upper bound
1      1.2 1.000001          1          2
2      1.9 1.000001          1          2

Cost Function:
function(x=NULL, index=NULL, fmsfunda=NULL){
  return(list(f=x[1]^2 + x[2]^2,
             g=c(),
             c=c(),
             gc=c(),
             index=index,
             this=list(costfargument=fmsfunda)))
}

Cost Function Argument(s):
[1] ""

Optimization:
- Status: "maxfuneval"
- Initial Cost Function Value: 5.050000
- Final Cost Function Value: 2.000004
- Number of Iterations (max): 90 (100)
- Number of Function Evaluations (max): 100 (100)

Simplex Information:

- Simplex at Initial Point:
Dimension: n=2
Number of vertices: nbve=3
  Vertex #1/3 : fv=5.050000e+00, x=1.200000e+00 1.900000e+00
  Vertex #2/3 : fv=7.610000e+00, x=2.000000e+00 1.900000e+00
  Vertex #3/3 : fv=5.440000e+00, x=1.200000e+00 2.000000e+00

- Simplex at Optimal Point:
Dimension: n=2
Number of vertices: nbve=3
  Vertex #1/3 : fv=2.000004e+00, x=1.000001e+00 1.000001e+00
  Vertex #2/3 : fv=2.000004e+00, x=1.000001e+00 1.000001e+00
  Vertex #3/3 : fv=2.000004e+00, x=1.000001e+00 1.000001e+00

```

3.4 Example 4: Optimization with nonlinear inequality constraints

In the following example, we solve Michalewicz's G_6 test problem using Box's methods [7]¹. This problem consists in minimizing: $G_6(x) = (x_1 - 10)^3 + (x_2 - 20)^3$, given the nonlinear constraints:

$$\begin{aligned} c1 &: (x_1 - 5)^2 + (x_2 - 5)^2 - 100 \geq 0 \\ c2 &: -(x_1 - 6)^2 - (x_2 - 5)^2 + 82.81 \geq 0 \\ \text{and bounds: } &13 \leq x_1 \leq 100, 0 \leq x_2 \leq 100. \end{aligned}$$

We begin by defining the `michalewicz` function, which takes 3 input arguments and return the value of the objective function and the constraint evaluations as the `f` and `c` elements of a list. `neldermead` creates a new `neldermead` object. Then we use `neldermead.configure` to configure the parameters of the problem, including the lower `-boundsmin` and upper `-boundsmax` bounds. The initial simplex is computed from `boxnbpoints` random points within the bounds. The variable simplex algorithm by Box is used, which corresponds to the `-method 'box'` option. `neldermead.search` finally performs the search for the minimum. The starting point ([15 4.99]) like all the vertices of the optimization simplex must be feasible, i.e. they must satisfy all constraints and bounds. Constraints are enforced by ensuring that all arguments of `c` in the cost function output are positive or null. Note that the boundaries were set to stricter ranges to limit the sensitivity of the solution to the initial guesses.

```
> michalewicz <- function(x=NULL, index=NULL, fmsfodata=NULL) {
+   f <- c()
+   c <- c()
+   if (index == 2 | index == 6)
+     f <- (x[1]-10)^3+(x[2]-20)^3
+
+   if (index == 5 | index == 6)
+     c <- c((x[1]-5)^2+(x[2]-5)^2 - 100,
+            82.81-((x[1]-6)^2+(x[2]-5)^2))
+   varargout <- list(f=f,
+                      g=c(),
+                      c=c,
+                      gc=c(),
+                      index=index,
+                      this=list(costfargument=fmsfodata))
+   return(varargout)
+ }
> set.seed(0)
> x0 <- transpose(c(15,4.99))
> nm <- neldermead()
> nm <- neldermead.configure(nm, '-numberofvariables', 2)
> nm <- neldermead.configure(nm, '-nbineqconst', 2)
> nm <- neldermead.configure(nm, '-function', michalewicz)
> nm <- neldermead.configure(nm, '-x0', x0)
> nm <- neldermead.configure(nm, '-maxiter', 300)
> nm <- neldermead.configure(nm, '-maxfunevals', 1000)
> nm <- neldermead.configure(nm, '-simplex0method', 'randbounds')
> nm <- neldermead.configure(nm, '-boxnbpoints', 3)
> nm <- neldermead.configure(nm, '-storehistory', TRUE)
```

¹Example suggested by Pascal Grandjeau

```

>   nm <- neldermead.configure(nm, '-method', 'box')
>   nm <- neldermead.configure(nm, '-boundsmin', c(13,0))
>   nm <- neldermead.configure(nm, '-boundsmax', c(20,10))
>   nm <- neldermead.search(nm)
>   summary(nm)

Number of Estimated Variable(s): 2

Estimated Variable(s):
  Initial      Final Lower bound Upper bound
1    15.00  14.0950000       13        20
2     4.99   0.8429608        0        10

Number of Inequality Constraints: 2

Cost Function:
function(x=NULL, index=NULL, fmsfodata=NULL){
  f <- c()
  c <- c()
  if (index == 2 | index ==6)
    f <- (x[1]-10)^3+(x[2]-20)^3

  if (index == 5 | index ==6)
    c <- c((x[1]-5)^2+(x[2]-5)^2 -100,
           82.81-((x[1]-6)^2+(x[2]-5)^2))
  varargout <- list(f=f,
                     g=c(),
                     c=c,
                     gc=c(),
                     index=index,
                     this=list(costfargument=fmsfodata))
  return(varargout)
}

Cost Function Argument(s):
[1] ""

Optimization:
- Status: "impossibleimprovement"
- Initial Cost Function Value: -3256.754501
- Final Cost Function Value: -6961.813876
- Number of Iterations (max): 236 (300)
- Number of Function Evaluations (max): 794 (1000)

Simplex Information:
- Simplex at Initial Point:
Dimension: n=2
Number of vertices: nbve=3

```

```

Vertex #1/3 : fv=-3.256755e+03, x=1.500000e+01 4.990000e+00
Vertex #2/3 : fv=-3.276394e+03, x=1.506683e+01 4.953517e+00
Vertex #3/3 : fv=-3.188984e+03, x=1.507561e+01 5.082317e+00

- Simplex at Optimal Point:
Dimension: n=2
Number of vertices: nbve=3
Vertex #1/3 : fv=-6.961814e+03, x=1.409500e+01 8.429608e-01
Vertex #2/3 : fv=-6.961814e+03, x=1.409500e+01 8.429608e-01
Vertex #3/3 : fv=-6.961814e+03, x=1.409500e+01 8.429608e-01

```

3.5 Example 5: Passing data to the cost function

In the following example, we use a simple example to illustrate how to pass user-defined arguments to a user-defined cost function. We try to find the mean and standard deviation of some normally distributed data using maximum likelihood (actually a modified negative log-likelihood approach)².

We begin by defining the `negLL` function, which takes 3 input arguments and return the value of the objective function. The random dataset is then generated and stored in the list `fmsfundata`. `neldermead` creates a new `neldermead` object. Then we use `neldermead.configure` to configure the parameters of the problem, including `costfargument`, set to `fmsfundata`, and the lower `-boundsmin` and upper `-boundsmax` bounds (the standard deviations has to be positive). The variable simplex algorithm by Box is used. `neldermead.search` finally performs the search for the minimum.

```

> negLL <- function(x=NULL, index=NULL, fmsfundata=NULL){
+   mn <- x[1]
+   sdv <- x[2]
+   out <- -sum(dnorm(fmsfundata$data, mean=mn, sd=sdv, log=TRUE))
+
+   return(list(f = out,
+             index = index,
+             this=list(costfargument=fmsfundata)))
+ }
> set.seed(12345)
> fmsfundata <- structure(
+   list(data=rnorm(500,mean=50,sd=2)),
+   class='optimbase.functionargs')
> x0 <- transpose(c(45,3))
> nm <- neldermead()
> nm <- neldermead.configure(nm,"-numberofvariables",2)
> nm <- neldermead.configure(nm,"-function",negLL)
> nm <- neldermead.configure(nm,"-x0",x0)
> nm <- neldermead.configure(nm,"-costfargument",fmsfundata)
> nm <- neldermead.configure(nm,"-maxiter",500)
> nm <- neldermead.configure(nm,"-maxfunevals",1500)
> nm <- neldermead.configure(nm,"-method","box")
> nm <- neldermead.configure(nm,"-storehistory",TRUE)
> nm <- neldermead.configure(nm,"-boundsmin",c(-100, 0))

```

²Example suggested by Mark Taper

```

>   nm <- neldermead.configure(nm, "-boundsmax", c(100, 100))
>   nm <- neldermead.search(this=nm)
>   summary(nm)

Number of Estimated Variable(s): 2

Estimated Variable(s):
  Initial      Final Lower bound Upper bound
1     45 50.164922       -100        100
2     3  1.978316         0        100

Cost Function:
function(x=NULL, index=NULL, fmsfunda=NULL){
  mn <- x[1]
  sdv <- x[2]
  out <- -sum(dnorm(fmsfunda$data, mean=mn, sd=sdv, log=TRUE))

  return(list(f = out,
             index = index,
             this=list(costfargument=fmsfunda)))
}

Cost Function Argument(s):
$data
 [1] 51.17106 51.41893 49.78139 49.09301 51.21177 46.36409 51.26020
 [8] 49.44763 49.43168 48.16136 49.76750 53.63462 50.74126 51.04043
[15] 48.49894 51.63380 48.22728 49.33684 52.24143 50.59745 51.55924
[22] 52.91157 48.71134 46.89373 46.80458 53.61020 49.03671 51.24076
[29] 51.22425 49.67538 51.62375 54.39367 54.09838 53.26489 50.50854
[36] 50.98238 49.35183 46.67590 53.53547 50.05160 52.25702 45.23928
[43] 47.87947 51.87428 51.70890 52.92146 47.17380 51.13481 51.16638
[50] 47.38640 48.91923 53.89539 50.10718 50.70333 48.65805 50.55591
[57] 51.38234 51.64759 54.29013 45.30611 50.29918 47.31494 51.10661
[64] 53.17993 48.82624 46.33525 51.77628 53.18698 51.03371 47.40866
[71] 50.10923 48.43070 47.90129 54.66102 52.80541 51.88520 51.65252
[78] 48.37692 50.95250 52.04252 51.29077 52.08629 49.39126 54.95422
[85] 51.94244 53.73420 51.34408 49.38409 51.07305 51.64974 48.07220
[92] 48.28983 53.77389 49.21636 48.03873 51.37466 48.98991 54.31544
[99] 48.80040 48.61091 50.44785 47.68755 50.84484 47.35049 50.28217
[106] 48.92790 49.37679 53.11222 49.10393 50.64225 47.53966 47.35188
[113] 52.52248 52.63846 49.83849 48.98982 49.89569 51.25772 54.36000
[120] 49.86197 53.08973 52.64290 50.64430 53.06191 49.15752 47.68236
[127] 46.30926 52.31465 45.75290 47.60794 53.28438 51.76731 51.04975
[134] 47.63068 55.31158 47.90417 47.97775 51.33784 50.25835 49.15485
[141] 47.71947 47.41257 48.81060 46.99837 50.03171 51.08034 46.90542
[148] 51.69931 51.79203 50.27738 46.76134 51.09680 50.39056 48.38700
[155] 49.78275 49.49811 53.39869 49.31140 50.13554 48.69886 49.02472
[162] 50.60630 49.51605 49.03653 48.01639 49.43870 51.26603 47.52036
[169] 53.52863 49.95264 50.39984 52.69439 50.07215 51.64916 46.59466

```

[176] 50.96190 54.96710 50.80273 50.43035 46.36858 48.17652 49.90191
 [183] 49.18923 52.26076 51.63093 50.15284 52.90749 50.74824 49.65819
 [190] 48.99557 51.08704 48.98963 51.57359 50.60190 52.62045 51.59687
 [197] 51.70172 49.11286 49.10645 50.02661 47.12771 48.74148 50.48704
 [204] 52.11672 51.66270 50.21042 46.51657 51.29049 50.19421 49.84653
 [211] 51.98390 48.28150 49.43684 54.13249 48.77689 50.63123 51.32059
 [218] 46.55560 45.73075 50.13789 51.73564 45.41991 49.69962 49.46244
 [225] 53.58266 51.34454 49.58140 50.02437 53.06823 50.15458 50.15688
 [232] 48.44148 50.33312 50.53065 51.78156 49.06422 51.51675 48.71653
 [239] 51.25534 50.49666 48.59985 48.86520 49.47721 47.87223 49.78726
 [246] 51.54221 55.49481 49.83213 51.08714 51.50572 48.38265 52.00224
 [253] 50.91211 47.13150 49.46939 51.28354 49.16996 49.08085 48.41501
 [260] 47.68292 51.42178 52.53520 49.71370 48.96994 52.96578 49.67482
 [267] 50.08342 50.96608 47.63975 48.67285 48.73070 48.59607 51.15370
 [274] 45.77384 50.52182 52.29425 50.02959 49.37652 48.08761 50.94683
 [281] 46.97227 50.32856 48.25827 53.18666 51.29320 50.71474 50.20479
 [288] 48.64947 51.94417 51.51174 49.14343 48.57215 49.61923 50.79973
 [295] 48.04431 50.36747 45.69938 48.75407 48.46912 50.92862 51.04456
 [302] 50.01959 49.11895 52.39898 49.76506 50.07642 52.38961 50.68792
 [309] 49.34185 53.34172 48.16388 49.82439 52.64059 53.46157 54.32519
 [316] 49.36854 48.84981 47.18729 54.53572 48.45829 50.76063 51.21027
 [323] 52.03935 50.94989 45.62811 51.86638 50.95087 50.78056 48.54534
 [330] 51.97311 52.84797 50.96946 50.69847 51.72025 50.80922 50.73409
 [337] 46.96160 53.09961 50.99976 50.92175 54.15342 49.38470 51.90474
 [344] 51.06558 49.80890 49.71587 47.63395 51.09064 44.83629 51.55780
 [351] 50.58588 49.82658 47.06728 47.83364 52.11547 49.27936 50.70119
 [358] 50.05652 50.94610 48.16169 49.24835 46.37433 50.57720 49.62075
 [365] 50.03572 51.30086 50.62051 53.33671 51.34523 49.44496 49.70795
 [372] 53.40286 50.94272 51.16340 51.33204 48.44220 52.32665 46.07091
 [379] 51.53834 54.51954 49.04546 49.79484 50.73739 48.92913 51.01320
 [386] 49.69889 51.80849 54.48407 47.60975 49.16295 51.59650 50.99634
 [393] 50.23912 49.26559 50.52466 50.52541 51.28148 50.61418 49.93374
 [400] 47.25050 51.25593 50.00429 50.56876 47.99644 48.76556 51.65639
 [407] 49.83036 49.13056 47.59033 47.95863 48.05754 49.67817 52.40937
 [414] 50.13349 48.23508 49.96016 50.65603 48.13874 47.73717 52.17246
 [421] 51.02848 50.58634 48.87469 50.41429 52.45615 49.13997 52.66382
 [428] 48.47347 52.46464 51.21812 48.35492 49.90470 50.34136 47.54986
 [435] 50.77467 50.98134 54.47825 51.78442 51.59787 53.87089 50.78850
 [442] 51.26504 50.20518 52.02042 52.42936 51.00174 48.18106 45.60558
 [449] 50.87709 47.94117 51.42616 52.05654 48.85873 49.13198 52.01063
 [456] 52.40709 52.99237 49.68680 48.12794 50.70508 47.42762 49.45495
 [463] 50.31383 48.23637 49.75620 48.28950 47.98854 48.17210 45.84353
 [470] 49.71871 52.59928 49.94126 45.52676 51.09006 51.66168 49.00484
 [477] 48.79795 48.97560 49.99014 49.80570 49.95193 49.74522 49.73623
 [484] 50.90748 47.18733 50.42186 51.50467 50.27676 50.31936 50.45687
 [491] 47.67443 51.70932 49.51581 45.96801 49.54462 50.44834 48.52635
 [498] 48.30658 49.77708 49.37680

```

attr(,"class")
[1] "optimbase.functionargs"

Optimization:
- Status: "impossibleimprovement"
- Initial Cost Function Value: 1858.501814
- Final Cost Function Value: 1050.592365
- Number of Iterations (max): 137 (500)
- Number of Function Evaluations (max): 268 (1500)

Simplex Information:

- Simplex at Initial Point:
Dimension: n=2
Number of vertices: nbve=3
  Vertex #1/3 : fv=1.858502e+03, x=4.500000e+01 3.000000e+00
  Vertex #2/3 : fv=1.599340e+03, x=4.600000e+01 3.000000e+00
  Vertex #3/3 : fv=1.630588e+03, x=4.500000e+01 4.000000e+00

- Simplex at Optimal Point:
Dimension: n=2
Number of vertices: nbve=3
  Vertex #1/3 : fv=1.050592e+03, x=5.016492e+01 1.978316e+00
  Vertex #2/3 : fv=1.050592e+03, x=5.016492e+01 1.978316e+00
  Vertex #3/3 : fv=1.050592e+03, x=5.016492e+01 1.978316e+00

```

3.6 Example 6: Direct grid search

In the following example, we use the Rosenbrock test case introduced as Example 2 to illustrate the direct grid search capacity of `neldermead`. We begin by defining the Rosenbrock function, which takes only one input argument and returns the value of the objective function. We request 6 points per dimension of the problem and set the range of search around the standard starting point [-1.2 1.0] by providing limits. `fmin.gridsearch` performs the search and return a table sorted by value of the cost function.

```

> rosenbrock <- function(x=NULL){
+   f <- 100*(x[2]-x[1]^2)^2+(1-x[1])^2
+ }
> x0 <- c(-1.2,1.0)
> npts <- 6
> xmin <- c(-2,-2)
> xmax <- c(2,2)
> grid <- fmin.gridsearch(fun=rosenbrock,x0=x0,xmin=xmin,xmax=xmax,npts=npts,alpha=alpha)

```

```

The grid contains 30 unique combinations.
Evaluating combination number: 1/30
Evaluating combination number: 2/30
Evaluating combination number: 3/30
Evaluating combination number: 4/30

```

```
Evaluating combination number: 5/30
Evaluating combination number: 6/30
Evaluating combination number: 7/30
Evaluating combination number: 8/30
Evaluating combination number: 9/30
Evaluating combination number: 10/30
Evaluating combination number: 11/30
Evaluating combination number: 12/30
Evaluating combination number: 13/30
Evaluating combination number: 14/30
Evaluating combination number: 15/30
Evaluating combination number: 16/30
Evaluating combination number: 17/30
Evaluating combination number: 18/30
Evaluating combination number: 19/30
Evaluating combination number: 20/30
Evaluating combination number: 21/30
Evaluating combination number: 22/30
Evaluating combination number: 23/30
Evaluating combination number: 24/30
Evaluating combination number: 25/30
Evaluating combination number: 26/30
Evaluating combination number: 27/30
Evaluating combination number: 28/30
Evaluating combination number: 29/30
Evaluating combination number: 30/30
```

```
> grid
```

	x1	x2	f	feasible
22	1.0	1	0.0	1
15	0.0	0	1.0	1
20	-1.0	1	4.0	1
24	-1.2	1	24.2	1
30	-1.2	2	36.2	1
16	1.0	0	100.0	1
28	1.0	2	100.0	1
9	0.0	-1	101.0	1
21	0.0	1	101.0	1
14	-1.0	0	104.0	1
26	-1.0	2	104.0	1
18	-1.2	0	212.2	1
10	1.0	-1	400.0	1
3	0.0	-2	401.0	1
27	0.0	2	401.0	1
29	2.0	2	401.0	1
8	-1.0	-1	404.0	1
25	-2.0	2	409.0	1
12	-1.2	-1	600.2	1

```

4   1.0 -2  900.0      1
23  2.0  1  901.0      1
2  -1.0 -2  904.0      1
19 -2.0  1  909.0      1
6   -1.2 -2 1188.2      1
17  2.0  0 1601.0      1
13 -2.0  0 1609.0      1
11  2.0 -1 2501.0      1
7   -2.0 -1 2509.0      1
5   2.0 -2 3601.0      1
1  -2.0 -2 3609.0      1

```

4 References

- [1] C.T. Kelley. *Iterative Methods for Optimization*. SIAM Frontiers in Applied Mathematics, Philadelphia, PA, 1999.
- [2] J.A. Guin. Discussion and correspondence: modification of the complex method of constrained optimization. *The Computer Journal*, 10(4):416–417, 1968.
- [3] J.A. Nelder and R. Mead. A Simplex Method for Function Minimization. *The Computer Journal*, 7(4):308–313, 1965.
- [4] M.J. Box. A New Method of Constrained Optimization and a Comparison With Other Methods. *The Computer Journal*, 1(8):42–52, 1965.
- [5] R. O'Neill. Algorithm AS47 - Function minimization using a simplex procedure. *Applied Statistics*, 20:338–345, 1971.
- [6] W. Spendley and G.R. Hext and F.R. Himsorth. Sequential Application of Simplex Designs in Optimisation and Evolutionary Operation. *Technometrics*, 4:441–461, 1962.
- [7] Z. Michalewicz and D.B. Fogel. *How to solve it: modern heuristics*, chapter Constraint-handling techniques, pages 231–270. Springer, 2004.

5 Dependencies of fminsearch

We illustrate in the figures below the network of functions of the **neldermead**, **optimbase**, and **optimsimplex** packages that are called from the **fminsearch** functions. This large network is broken down in 6 plots, which are shown in the order functions are called. Green boxes represent functions that are not expanded on a given plot but on a previous or later one.

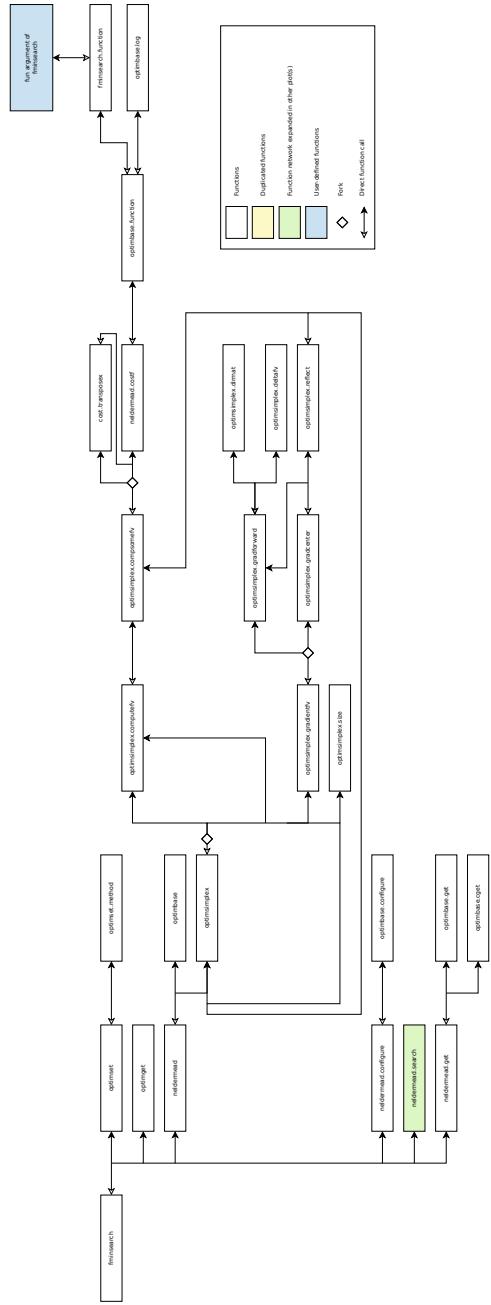


Figure 1: fminsearch function network (1/6)

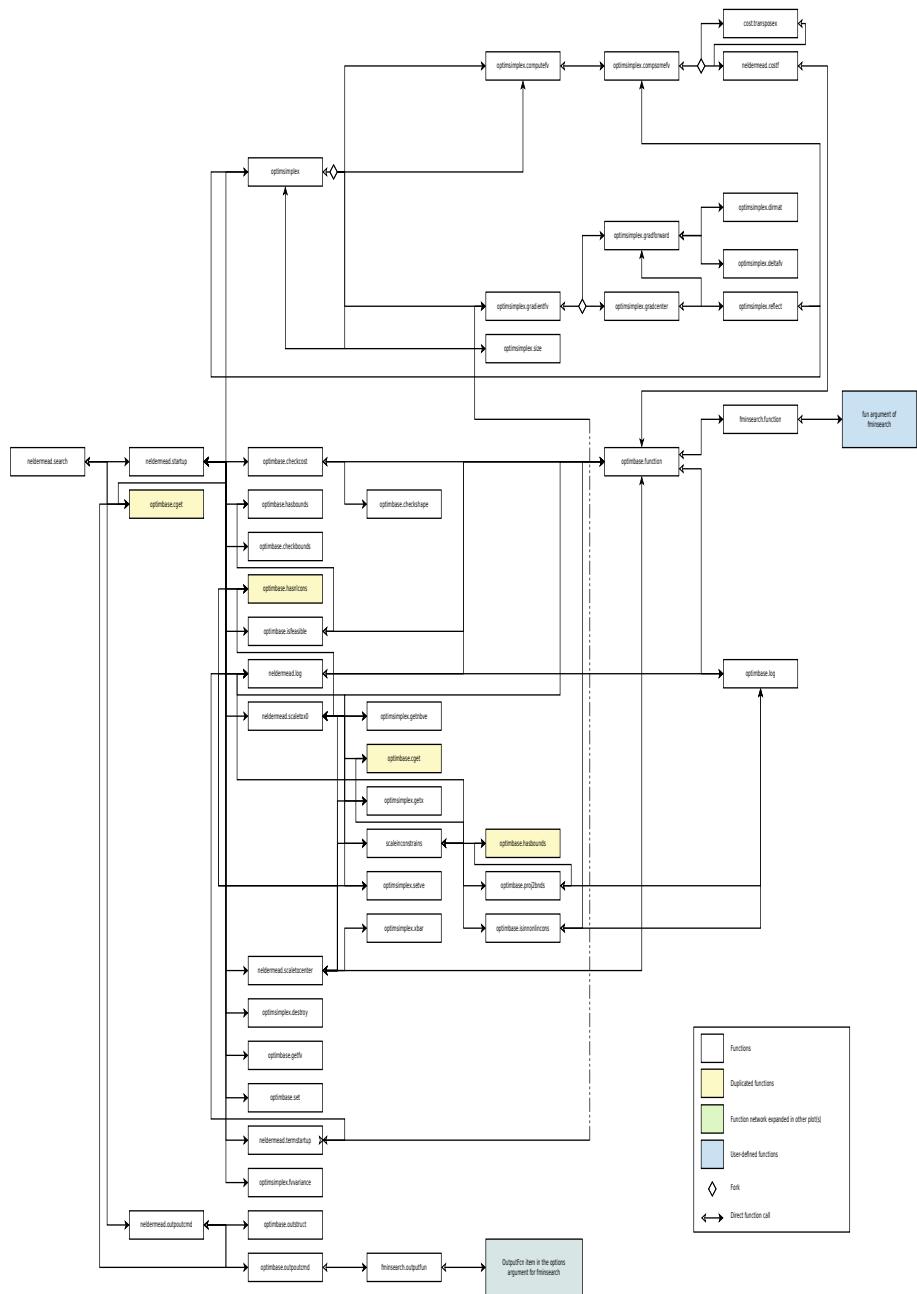


Figure 2: fminsearch function network (2/6)

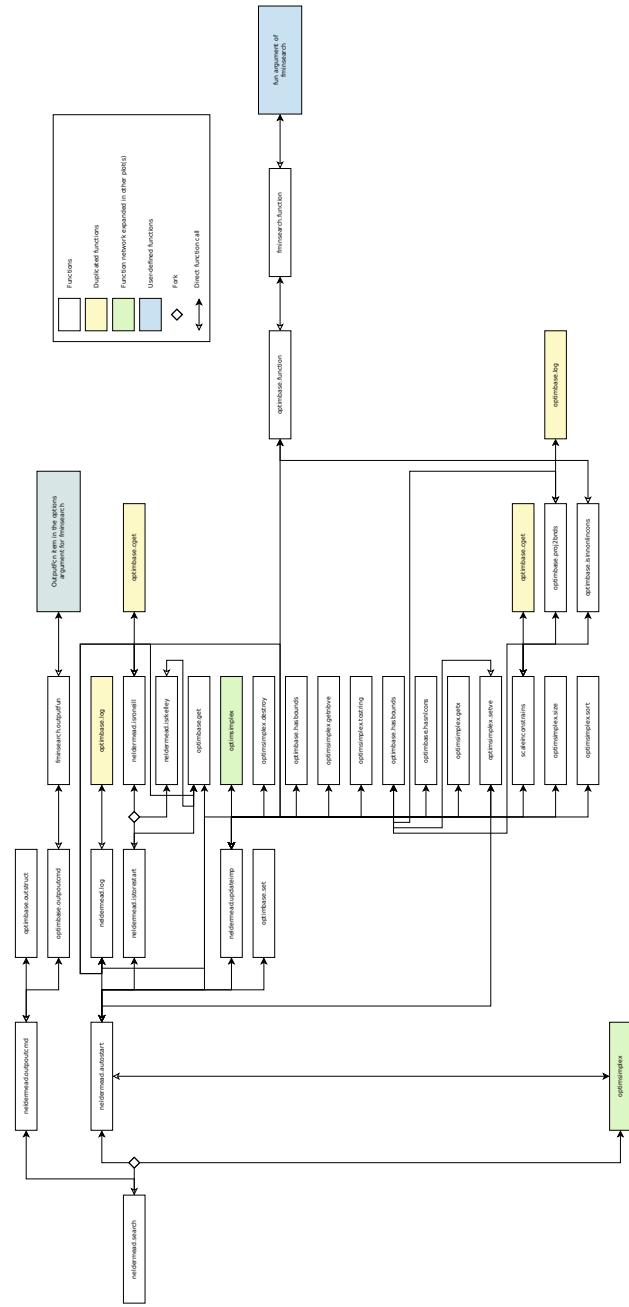


Figure 3: fminsearch function network (3/6)

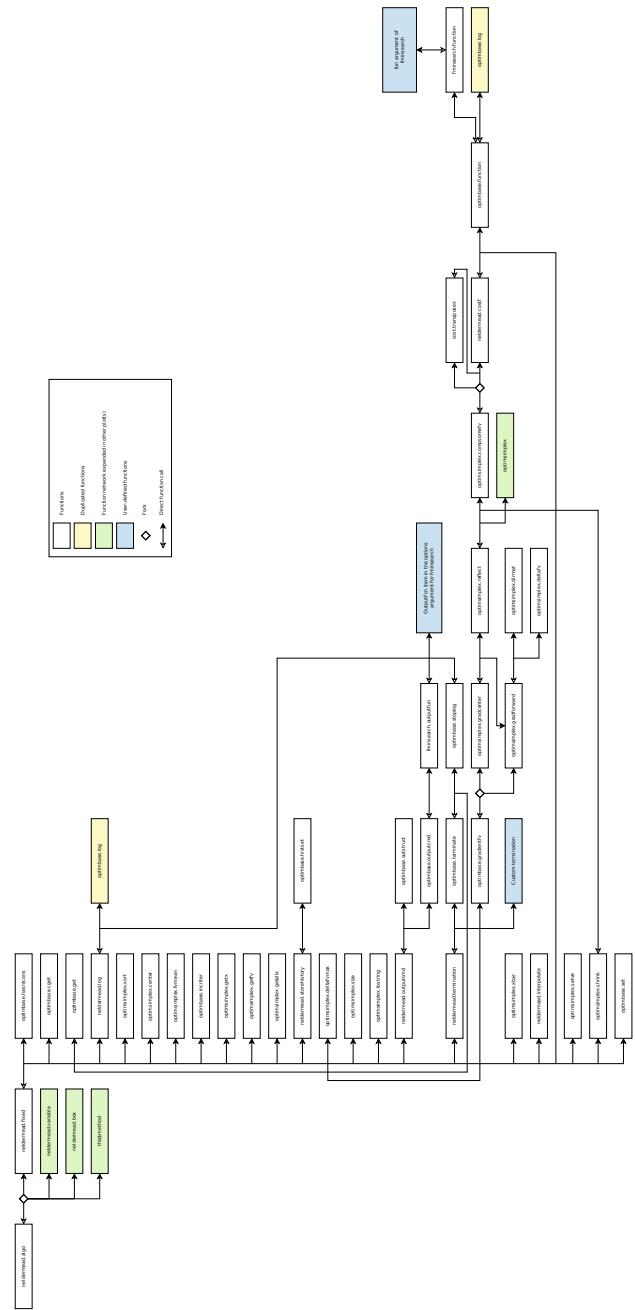


Figure 4: fminsearch function network (4/6)

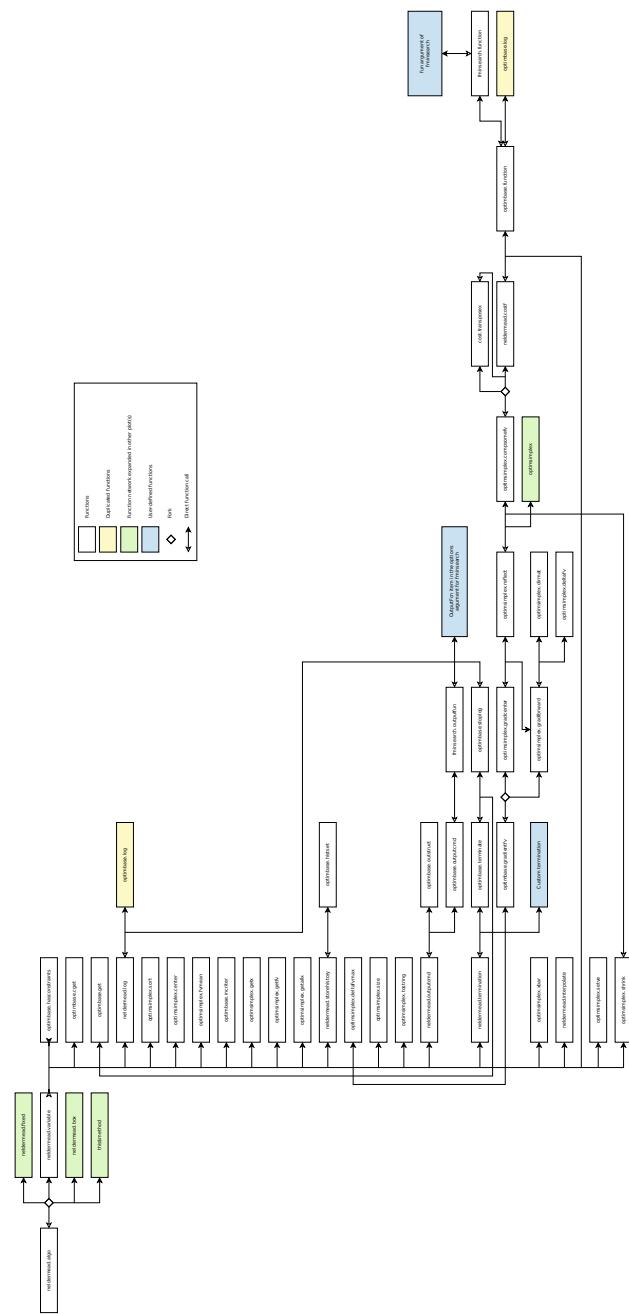


Figure 5: fminsearch function network (5/6)

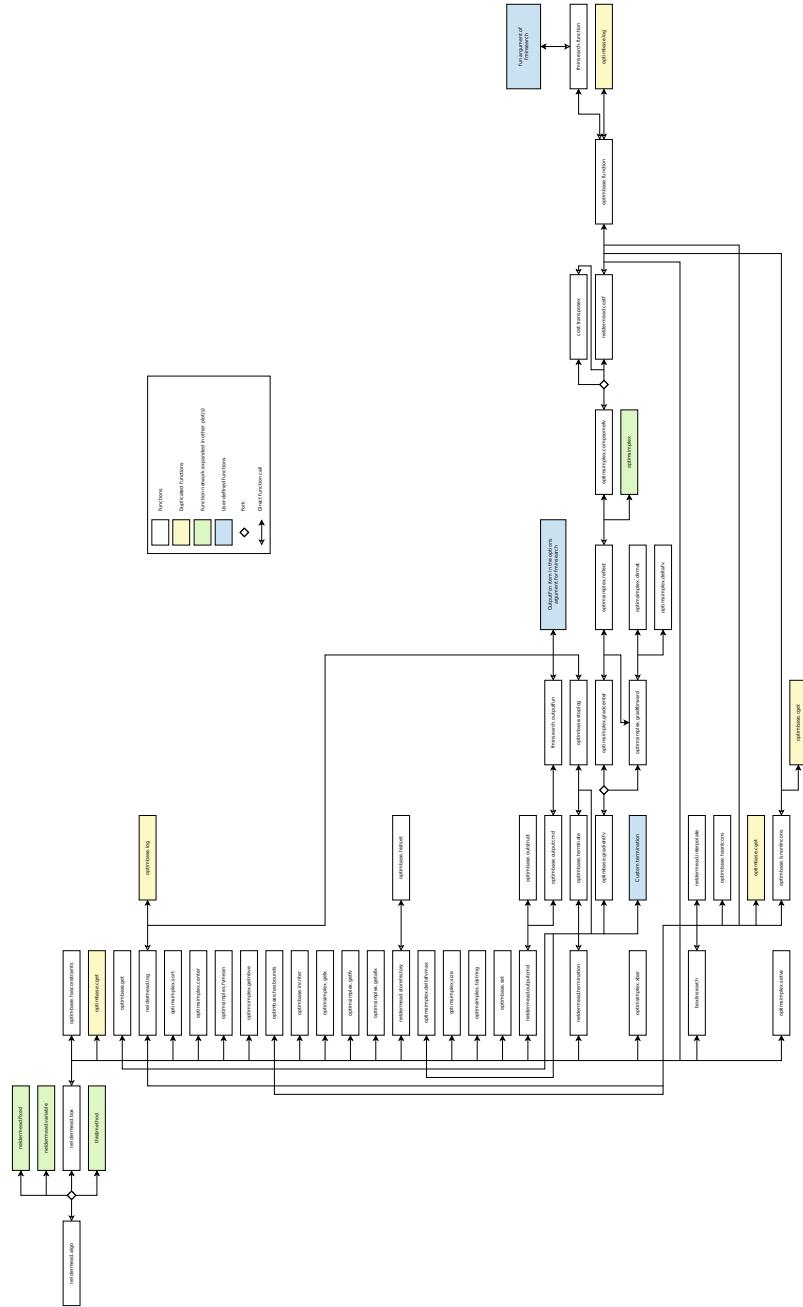


Figure 6: `fminsearch` function network (6/6)

6 Help on neldermead functions

neldermead-package *R port of the Scilab neldermead module*

Description

The goal of this package is to provide a Nelder-Mead direct search optimization method. That Nelder-Mead algorithm may be used in the following optimization context:

- there is no need to provide the derivatives of the objective function,
- the number of parameters is small (up to 10-20),
- there are bounds and/or non linear constraints.

Design

This package provides the following components:

- **neldermead** provides various Nelder-Mead variants and manages for Nelder-Mead specific settings, such as the method to compute the initial simplex, the specific termination criteria,
- **fminsearch** provides a simplified Nelder-Mead algorithm. Specific termination criteria, initial simplex and auxiliary settings are automatically configured.
- **fminbnd** provides a simplified Box algorithm, ie the equivalent of **fminsearch** for unconstrained search.
- **optimset**, **optimget** provide commands to emulate their Scilab counterparts.
- **optimplotfuncount**, **optimplotx** and **optimplotfval** provide plotting features for the **fminsearch** function (Not implemented yet).
- **nmplot** provides a high-level component which provides directly output pictures for Nelder-Mead algorithm. (Not implemented yet).

The current component is based on the following packages

- **optimbase**: provides an abstract class for a general optimization component, including the number of variables, the minimum and maximum bounds, the number of non linear inequality constraints, the loggin system, various termination criteria, the cost function, etc...
- **optimsimplex**: provides a class to manage a simplex made of an arbitrary number of vertices, including the computation of a simplex by various methods (axes, regular, Pfeffer's, randomized bounds), the computation of the size by various methods (diameter, sigma+, sigma-, etc...),

Features

The following is a list of features the Nelder-Mead prototype algorithm currently provides:

- Provides 3 algorithms, including
 - the fixed shape algorithm of Spendley et al.,
 - the variable shape algorithm of Nelder and Mead,

- Box's 'complex' algorithm managing bounds and nonlinear inequality constraints based on arbitrary number of vertices in the simplex.
- Manage various simplex initializations:
 - initial simplex given by user,
 - initial simplex computed with a length and along the coordinate axes,
 - initial regular simplex computed with formula of Spendley et al.,
 - initial simplex computed by a small perturbation around the initial guess point.
- Manage cost function:
 - optional additional argument,
 - direct communication of the task to perform: cost function or inequality constraints.
- Manage various termination criteria, including maximum number of iterations, tolerance on function value (relative or absolute):
 - tolerance on x (relative or absolute),
 - tolerance on standard deviation of function value (original termination criteria in Box 1965),
 - maximum number of evaluations of cost function,
 - absolute or relative simplex size.
- Manage the history of the convergence, including:
 - history of function values,
 - history of optimum point,
 - history of simplices,
 - history of termination criteria.
- Provide a plot command which allows to graphically see the history of the simplices toward the optimum (Not yet implemented).
- Provide query features for the status of the optimization process: number of iterations, number of function evaluations, status of execution, function value at initial point, function value at optimal point, etc...
- Kelley restart based on simplex gradient.
- O'Neill restart based on factorial search around optimum.

Details

Package:	neldermead
Type:	Package
Version:	1.0-8
Date:	2014-01-29
License:	CeCILL-2
LazyLoad:	yes

See `vignette('neldermead', package='neldermead')` for more information.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

References

'Sequential Application of Simplex Designs in Optimisation and Evolutionary Operation', Spendley, W. and Hext, G. R. and Himsworth, F. R., American Statistical Association and American Society for Quality, 1962

'A Simplex Method for Function Minimization', Nelder, J. A. and Mead, R., The Computer Journal, 1965

'A New Method of Constrained Optimization and a Comparison With Other Methods', M. J. Box, The Computer Journal 1965 8(1):42-52, 1965 by British Computer Society

'Discussion and correspondence: modification of the complex method of constrained optimization', J. A. Guin, The Computer Journal, 1968

'Detection and Remediation of Stagnation in the Nelder-Mead Algorithm Using a Sufficient Decrease Condition', Kelley C. T., SIAM J. on Optimization, 1999

'Iterative Methods for Optimization', C. T. Kelley, SIAM Frontiers in Applied Mathematics, 1999

'Algorithm AS47 - Function minimization using a simplex procedure', O'Neill, R., Applied Statistics, 1971

See Also

`optimbase optimsimplex`

`costf.transpose()` *Cost Function Call*

Description

Call the cost function after transposition of the value of the point estimate `x`, so that the input row vector, given by `optimsimplex`, is transposed into a column vector as required by the cost function.

Usage

`costf.transpose(x = NULL, this = NULL)`

Arguments

- | | |
|-------------------|---|
| <code>x</code> | The point estimate provide as a row matrix. |
| <code>this</code> | A neldermead object. |

Value

Return the value of the cost function (called by `neldermead.costf.`)

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sébastien Bihorel (<sb.pmlab@gmail.com>)

See Also

`neldermead.costf`

`fmin.gridsearch`

Grid evaluation of an unconstrained cost function

Description

Evaluate an unconstrained cost function on a grid of points around a given initial point estimate.

Usage

```
fmin.gridsearch(fun = NULL, x0 = NULL, xmin = NULL,  
                 xmax = NULL, npts = 3, alpha = 10)
```

Arguments

<code>fun</code>	An unconstrained cost function returning a numeric scalar, similar to those used in the <code>fminsearch</code> function.
<code>x0</code>	The initial point estimate, provided as a numeric vector.
<code>xmin</code>	Optional: a vector of lower bounds.
<code>xmax</code>	Optional: a vector of upper bounds.
<code>npts</code>	An integer scalar greater than 2, indicating the number of evaluation points will be used on each dimension to build the search grid.
<code>alpha</code>	A vector of numbers greater than 1, which give the factor(s) used to calculate the evaluation range of each dimension of the search grid (see Details). If <code>alpha</code> length is lower than that of <code>x0</code> , elements of <code>alpha</code> are recycled. If its length is higher than that of <code>x0</code> , <code>alpha</code> is truncated.

Details

`fmin.gridsearch` evaluates the cost function at each point of a grid of `npts^length(x0)` points. If lower (`xmin`) and upper (`xmax`) bounds are provided, the range of evaluation points is limited by those bounds and `alpha` is not used. Otherwise, the range of evaluation points is defined as `[x0/alpha, x0*alpha]`.

The actual evaluation of the cost function is delegated to `optimbase.gridsearch`.

Value

Return a data.frame with the coordinates of the evaluation point, the value of the cost function and its feasibility. Because the cost function is unconstrained, it is always feasible. The data.frame is ordered by feasibility and increasing value of the cost function.

Author(s)

Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

`fminsearch`, `optimbase.gridsearch`

`fminsearch.function` *fminsearch Cost Function Call*

Description

This function calls the cost function and makes it match neldermead requirements. It is used in the `fminsearch` function as the `function` element of the neldermead object (see `?neldermead` and `?neldermead.configure`).

Usage

```
fminsearch.function(x = NULL, index = NULL, fmsfodata = NULL)
```

Arguments

- | | |
|------------------------|--|
| <code>x</code> | A single column vector of parameter estimates. |
| <code>index</code> | An integer variable set to 2, indicating that only the cost function is to be computed by the algorithm. |
| <code>fmsfodata</code> | An object of class 'optimbase.functionargs' and with (at least) a <code>fun</code> element, which contains the user-defined cost function. |

Value

Returns a list with the following elements:

- `f` The value of the cost function at the current point estimate.
- `index` The same `index` variable.
- `this` A list with a single element `costargument` which contains `fmsfodata`.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

`fminsearch`, `neldermead`, `neldermead.configure`,

`fminbnd.outputfun` *fminbnd Output Function Call*

Description

This function calls the output function and make it match neldermead requirements. It is used in the `fminbnd` function as the `outputcommand` element of the `neldermead` object (see `?neldermead` and `?neldermead.configure`).

Usage

```
fminbnd.outputfun(state = NULL, data = NULL, fmsdata = NULL)
```

Arguments

<code>state</code>	The current state of the algorithm either 'init', 'iter' or 'done'.
<code>data</code>	The data at the current state. This is an object of class 'neldermead.data', i.e. a list with the following elements: <ul style="list-style-type: none"><code>x</code> The current parameter estimates.<code>fval</code> The current value of the cost function.<code>simplex</code> The current simplex object.<code>iteration</code> The number of iterations performed.<code>funcount</code> The number of function evaluations.<code>step</code> The type of step in the previous iteration.
<code>fmsdata</code>	This is an object of class 'optimbase.functionargs' which contains specific data of the <code>fminbnd</code> algorithm: <ul style="list-style-type: none"><code>Display</code> what to display<code>OutputFcn</code> the array of output functions<code>PlotFcns</code> the array of plot functions

Value

This function does not return any data, but execute the output function(s).

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

`fminbnd`, `neldermead`, `neldermead.configure`,

fminsearch

Computation of the unconstrained minimum of given function with the Nelder-Mead algorithm.

Description

This function searches for the unconstrained minimum of a given cost function. The provided algorithm is a direct search algorithm, i.e. an algorithm which does not use the derivative of the cost function. It is based on the update of a simplex, which is a set of $k \geq n+1$ vertices, where each vertex is associated with one point and one function value. This algorithm is the Nelder-Mead algorithm. This function is based on a specialized use of the more general **neldermead** function bundle. Users who want to have a more flexible solution based on direct search algorithms should consider using the **neldermead** functions instead of the **fminsearch** function.

Usage

```
fminsearch(fun = NULL, x0 = NULL, options = NULL, verbose=FALSE)
```

Arguments

fun	A cost function return a numeric scalar.
x0	A numerical vector of initial guesses (length n).
options	A list of optimization options, which drives the behaviour of fminsearch . These options must be set with the optimset function (see ?optimset) which returns a list with the following elements: <ul style="list-style-type: none">MaxIter The maximum number of iterations. The default is $200 * n$.MaxFunEvals The maximum number of evaluations of the cost function. The default is $200 * n$.TolFun The absolute tolerance on function value. The default value is $1.e-4$.TolX The absolute tolerance on simplex size. The default value is $1.e-4$.Display The verbose level.OutputFcn The output function, or a list of output functions called at the end of each iteration. The default value is NULL.PlotFcns The plot function, or a list of plotput functions called at the end of each iteration. The default value is empty.
verbose	The verbose option, controlling the amount of messages.

Details

Termination criteria

In this section, we describe the termination criteria used by **fminsearch**. The criteria is based on the following variables:

ssize the current simplex size,

shiftfv the absolute value of the difference of function value between the highest and lowest vertices.

If both **ssize < options\$TolX** and **shiftfv < options\$TolFun** conditions are true, then the iterations stop. The size of the simplex is computed using the 'sigmaplus' method of the **optim-simplex** package. The 'sigmamplus' size is the maximum length of the vector from each vertex to the first vertex. It requires one loop over the vertices of the simplex.

The initial simplex

The **fminsearch** algorithm uses a special initial simplex, which is an heuristic depending on the initial guess. The strategy chosen by **fminsearch** corresponds to the content of **simplex0method** element of the **neldermead** object (set to 'pfeffer'). It is applied using the content of the **simplex0deltausual** (0.05) and **simplex0deltazero** (0.0075) elements. Pfeffer's method is an heuristic which is presented in 'Global Optimization Of Lennard-Jones Atomic Clusters' by Ellen Fan. It is due to L. Pfeffer at Stanford. See in the help of **optimsimplex** for more details.

The number of iterations

In this section, we present the default values for the number of iterations in **fminsearch**.

The **options** input argument is an optional list which can contain the **MaxIter** field, which stores the maximum number of iterations. The default value is $200n$, where n is the number of variables. The factor 200 has not been chosen by chance, but is the result of experiments performed against quadratic functions with increasing space dimension. This result is presented in 'Effect of dimensionality on the Nelder-mead simplex method' by Lixing Han and Michael Neumann. This paper is based on Lixing Han's PhD, 'Algorithms in Unconstrained Optimization'. The study is based on numerical experiments with a quadratic function where the number of terms depends on the dimension of the space (i.e. the number of variables). Their study showed that the number of iterations required to reach the tolerance criteria is roughly $100n$. Most iterations are based on inside contractions. Since each step of the Nelder-Mead algorithm only require one or two function evaluations, the number of required function evaluations in this experiment is also roughly $100n$.

Output and plot functions

The **optimset** function can be used to configure one or more output and plot functions. The output or plot function is expected to have the following definition:

```
myfun <- function(x , optimValues , state)
```

The input arguments **x**, **optimValues** and **state** are described in detail in the **optimset** help page. The **optimValues\$procedure** field represents the type of step performed at the current iteration and can be equal to one of the following strings:

- " (the empty string),
- 'initial simplex',
- 'expand',
- 'reflect',
- 'contract inside',
- 'contract outside'.

Value

Return a list with the following fields:

x The vector of n numeric values, minimizing the cost function.

fval The minimum value of the cost function.

exitflag The flag associated with exist status of the algorithm. The following values are available:

-1 The maximum number of iterations has been reached.

0 The maximum number of function evaluations has been reached.

1 The tolerance on the simplex size and function value delta has been reached. This signifies that the algorithm has converged, probably to a solution of the problem.

output A list which stores detailed information about the exit of the algorithm. This list contains the following fields:

algorithm A string containing the definition of the algorithm used, i.e. 'Nelder-Mead simplex direct search'.

funcCount The number of function evaluations.

iterations The number of iterations.

message A string containing a termination message.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

References

'Sequential Application of Simplex Designs in Optimisation and Evolutionary Operation', Spendley, W. and Hext, G. R. and Himsworth, F. R., American Statistical Association and American Society for Quality, 1962

'A Simplex Method for Function Minimization', Nelder, J. A. and Mead, R., The Computer Journal, 1965

'Iterative Methods for Optimization', C. T. Kelley, SIAM Frontiers in Applied Mathematics, 1999

'Algorithm AS47 - Function minimization using a simplex procedure', O'Neill, R., Applied Statistics, 1971

'Effect of dimensionality on the nelder-mead simplex method', Lixing Han and Michael Neumann, Optimization Methods and Software, 21, 1, 1–16, 2006.

'Algorithms in Unconstrained Optimization', Lixing Han, Ph.D., The University of Connecticut, 2000.

'Global Optimization Of Lennard-Jones Atomic Clusters' Ellen Fan, Thesis, February 26, 2002, McMaster University

See Also

`optimset`

Examples

```
#In the following example, we use the fminsearch function to compute the minimum
#of the Rosenbrock function. We first define the function 'banana', and then use
#the fminsearch function to search the minimum, starting with the initial guess
#(-1.2, 1.0). In this particular case, 85 iterations are performed with 159
#function evaluations
banana <- function(x){
  y <- 100*(x[2]-x[1]^2)^2 + (1-x[1])^2
}
sol <- fminsearch(banana, c(-1.2,1))
sol

#In the following example, we configure the absolute tolerance on the size of
#the simplex to a larger value, so that the algorithm performs less iterations.
#Since the default value of 'TolX' for the fminsearch function is 1.e-4, we
#decide to use 1.e-2. The optimset function is used to create an optimization
#option list and the field 'TolX' is set to 1.e-2. The options list is then
#passed to the fminsearch function as the third input argument. In this
#particular case, the number of iterations is 70 with 130 function evaluations.

opt <- optimset(TolX=1.e-2)
sol <- fminsearch(banana, c(-1.2,1), opt)
sol

#In the following example, we want to produce intermediate outputs of the
#algorithm. We define the outfun function, which takes the current point x as
#input argument. The function plots the current point into the current graphic
>window with the plot function. We use the 'OutputFcn' feature of the optimset
#function and set it to the output function. Then the option list is passed
#to the fminsearch function. At each iteration, the output function is called
#back, which creates and update a plot. While this example creates a 2D plot,
#the user may customized the output function so that it writes a message in
#the console, write some data into a data file, etc... The user can distinguish
#between the output function (associated with the 'OutputFcn' option) and the
#plot function (associated with the 'PlotFcns' option). See the optimset for
#more details on this feature.

outfun <- function(x, optimValues, state){
  plot(x[1],x[2],xlim=c(-1.5,1.5),ylim=c(-1.5,1.5))
  par(new=TRUE)
}
opt <- optimset(OutputFcn=outfun)
sol <- fminsearch(banana, c(-1.2,1), opt)
sol

#The 'Display' option allows to get some input about the intermediate steps of
#the algorithm as well as to be warned in case of a convergence problem.
#In the following example, we present what happens in case of a convergence
#problem. We set the number of iterations to 10, instead of the default 400
#iterations. We know that 85 iterations are required to reach the convergence
#criteria. Therefore, the convergence criteria is not met and the maximum number
#of iterations is reached.
```

```

opt <- optimset(MaxIter=10)
sol <- fminsearch(banana, c(-1.2,1), opt)

#Since the default value of the 'Display' option is 'notify', a message is
#generated, which warns the user about a possible convergence problem. The
#previous script produces the following output.
# Exiting: Maximum number of iterations has been exceeded
#           - increase MaxIter option.
#           Current function value: 4.1355598

#In the following example, we present how to display intermediate steps used by
#the algorithm. We simply set the 'Display' option to the 'iter' value. This
#option allows to see the number of function evaluations, the minimum function
#value and which type of simplex step is used for the iteration.
opt <- optimset(Display='iter')
sol <- fminsearch(banana, c(-1.2,1), opt)
sol

```

`neldermead.algo` *Nelder-Mead Algorithm*

Description

`neldermead.algo` performs an optimization without restart using the method associated with the `method` element of the `neldermead` object; `neldermead.fixed`, `neldermead.variable`, `neldermead.box`, `boxlinesearch`, `neldermead.storehistory`, `neldermead.termination`, and `neldermead.interpolate` are utility functions for `neldermead.algo`.

Usage

```

neldermead.algo(this = NULL)
neldermead.fixed(this = NULL)
neldermead.variable(this = NULL)
neldermead.box(this = this)
boxlinesearch(this = NULL, n = NULL, xbar = NULL, xhigh = NULL, fhigh = NULL,
             rho = NULL)
neldermead.storehistory(this = NULL, n = NULL, fopt = NULL, xo = NULL,
                         fv = NULL, xco = NULL)
neldermead.termination(this = NULL, fvinitial = NULL, oldfvmean = NULL,
                       newfvmean = NULL, previousxo = NULL,
                       currentxo = NULL, simplex = NULL)
neldermead.interpolate(x1 = NULL, x2 = NULL, fac = NULL)

```

Arguments

- | | |
|-------------------|-----------------------------------|
| <code>this</code> | A <code>neldermead</code> object. |
| <code>n</code> | Number of variables. |

xbar	The centroid.
xhigh	The high point.
fhigh	The value of the cost function at xhigh .
rho	The reflection factor.
fopt	The current value of the function at the current optimum point estimate.
xopt	The current optimum point estimate.
fv	The function values, with size nbve x 1.
xcoords	Matrix of size n x n+1, coordinates of the n+1 vertices
fvinitial	The initial cost function value.
oldfvmean	The old cost function value average on the simplex.
newfvmean	The new cost function value average on the simplex.
previousxopt	The previous point estimate.
currentxopt	The current point estimate.
simplex	The simplex. The best point estimate in the simplex is expected to be stored at 1, while the worst point estimate in the simplex is expected to be stored at n+1.
x1	The first reference point estimate to perform the interpolation.
x2	The second reference point estimate to perform the interpolation.
fac	A factor to perform the interpolation.

Details

neldermead.fixed The simplex algorithm with fixed size simplex. We implement the following 'rules' of the method of Spendley et al.

- Rule 1 is strictly applied, but the reflection is done by reflection of the high point, since we minimize a function instead of maximizing it, like Spendley.
- Rule 2 is NOT implemented, as we expect that the function evaluation is not subject to errors.
- Rule 3 is applied, i.e. reflection with respect to next to high point. A shrink step is included, with shrinkage factor sigma.

Rule 1. Ascertain the lowest reading y_i of $y_1 \dots Y_{k+1}$. Complete a new simplex S_p by excluding the point V_p corresponding to y_i , and replacing it by V^* defined as above.

Rule 2. If a result has occurred in $(k + 1)$ successive simplexes, and is not then eliminated by application of Rule 1, do not move in the direction indicated by Rule 1, or at all, but discard the result and replace it by a new observation at the same point.

Rule 3. If y_i is the lowest reading in S_o , and if the next observation made, y^* , is the lowest reading in the new simplex S_p , do not apply Rule 1 and return to S_o from S_p . Move out of S_p by rejecting the second lowest reading (which is also the second lowest reading in S_o).

neldermead.variable The original Nelder-Mead algorithm, with variable-size simplex.

neldermead.box The Nelder-Mead algorithm, with variable-size simplex and modifications by Box for bounds and inequality constraints.

boxlinesearch Called by **neldermead.box**, i.e. Box's method. Perform a line search from **xbar**, on the line (**xhigh,xbar**). The reflected point estimate satisfies the following constraints:

- **fr** < **fhigh**
- **xr** satisfies the bounds constraints
- **xr** satisfies the nonlinear positive inequality constraints
- **xr** satisfies the linear positive inequality constraints

The method is based on projection and scaling toward the centroid.

neldermead.storehistory Store the optimization history into the **neldermead** object.

neldermead.termination Determine if the algorithm must continue or terminate. The function uses the cost function average in the simplex instead of the best cost function value. This is because the function average changes at each iteration. Instead, the best function value has a step-by-step evolution and may not change between two successive iterations, leading to a stop of the algorithm.

neldermead.interpolate Compute the point estimate **xi** as an interpolation between **x1** and **x2**, as follows: $xi = (1+fac)x1 - fac*x2$

Value

neldermead.fixed, **neldermead.variable**, and **neldermead.box** Return the updated neldermead object, containing the optimum point estimate.

boxlinesearch Return a list with the following elements:

this The updated neldermead object.

status TRUE if the search is successful, FALSE otherwise.

xr The reflected point estimate.

fr The value of the cost function at **xr**.

neldermead.storehistory Return the updated neldermead object.

neldermead.termination Return a list with the following elements:

this The updated neldermead object

terminate TRUE if the algorithm terminates, FALSE if the algorithm must continue.

status The termination status: 'continue', 'maxiter', 'maxfuneval', 'tolf', 'tolx', 'tolsize', 'tolsizedeltafv', 'kelleystagnation', 'tolboxf', 'tolvariance' or the user-defined termination status.

neldermead.interpolate Return a new point estimate, i.e. a column vector.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sébastien Bihorel (<sb.pmlab@gmail.com>)

neldermead.configure *Neldermead Object Configuration*

Description

Configure the current neldermead object with the given value for the given key.

Usage

```
neldermead.configure(this = NULL, key = NULL, value = NULL)
```

Arguments

this	The current neldermead object.
key	The key to configure. See details for the list of possible keys.
value	The value to assign to the key.

Details

neldermead.configure sets the content of the **key** element of the neldermead object **this** to **value**. If **key** is a sub-element of **this\$optbase**, **value** is assigned by **optimbase.configure**.

The main available keys are the following:

- '-verbose'** Set to 1 to enable verbose logging.
- '-verbosetermination'** Set to 1 to enable verbose termination logging.
- '-x0'** The initial guess, as a $n \times 1$ column vector, where n is the number of variables.
- '-maxfunevals'** The maximum number of function evaluations. If this criteria is triggered during optimization, the status of the optimization is set to 'maxfuneval'.
- '-maxiter'** The maximum number of iterations. If this criteria is triggered during optimization, the status of the optimization is set to 'maxiter'.option
- '-tolfunabsolute'** The absolute tolerance for the function value.
- '-tolfunrelative'** The relative tolerance for the function value.
- '-tolfunmethod'** The method used for the tolerance on function value in the termination criteria. The following values are available: TRUE, FALSE. If this criteria is triggered, the status of the optimization is set to 'tolf'.
- '-tolxabsolute'** The absolute tolerance on x .
- '-tolxrelative'** The relative tolerance on x .
- '-tolxmethod'** The method used for the tolerance on x in the termination criteria. The following values are available: TRUE, FALSE. If this criteria is triggered during optimization, the status of the optimization is set to 'tolx'.
- '-function'** The objective function, which computes the value of the cost and the non linear constraints, if any. See `vignette('neldermead', package='neldermead')` for the details of the communication between the optimization system and the cost function.

'-costfargument' An additionnal argument, passed to the cost function.

'-outputcommand' A command which is called back for output. See `vignette('neldermead', package='neldermead')` for the details of the communication between the optimization system and the output command function.

'-outputcommandarg' An additionnal argument, passed to the output command.option

'-numberofvariables' The number of variables to optimize.

'-storehistory' Set to TRUE to enable the history storing.

'-boundsmin' The minimum bounds for the parameters.

'-boundsmax' The maximum bounds for the parameters.

'-nbineqconst' The number of inequality constraints.

'-method' The name of the algorithm to use. The following methods are available:

- 'fixed'** the fixed simplex shape algorithm of Spendley et al. This algorithm is for unconstrained problems (i.e. bounds and non linear constraints are not taken into account)
- 'variable'** the variable simplex shape algorithm of Nelder and Mead. This algorithm is for unconstrained problems (i.e. bounds and non linear constraints are not taken into account)
- 'box'** Box's complex algorithm. This algorithm takes into account bounds and nonlinear inequality constraints.
- 'mine'** the user-defined algorithm, associated with the `mymethod` element. See `vignette('neldermead', package='neldermead')` for details.

'-simplex0method' The method to use to compute the initial simplex. The first vertex in the simplex is always the initial guess associated with the `x0` element. The following methods are available:

- 'given'** The coordinates associated with the `coords0` element are used to compute the initial simplex, with arbitrary number of vertices. This allows the user to setup the initial simplex by a specific method which is not provided by the current package (for example with a simplex computed from a design of experiments). This allows also to configure the initial simplex so that a specific behaviour of the algorithm is to be reproduced (for example the Mac Kinnon test case). The given matrix is expected to have `nbve` rows and `n` columns, where `n` is the dimension of the problem and `nbve` is the number of vertices.
- 'axes'** The simplex is computed from the coordinate axes and the length associated with the `simplex0length` element.
- 'spendley'** The simplex is computed so that it is regular with the length associated with the `simplex0length` element (i.e. all the edges have the same length).
- 'pfeffer'** The simplex is computed from an heuristic, in the neighborhood of the initial guess. This initial simplex depends on the `-simplex0deltausual` and `-simplex0deltazero`.
- 'randbounds'** The simplex is computed from the bounds and a random number. This option is available only if bounds are available: if bounds are not available, an error is generated. This method is usually associated with Box's algorithm. The number of vertices in the simplex is taken from the `boxnbpoints` element.
- '-coords0'** The coordinates of the vertices of the initial simplex. If the `simplex0method` element is set to 'given', these coordinates are used to compute the initial simplex. This matrix is expected to have shape `nbve x n`, where `nbve` is the number of vertices and `n` is the number of variables.

- '-simplex0length'** The length to use when the initial simplex is computed with the 'axes' or 'spendley' methods. If the initial simplex is computed from 'spendley' method, the length is expected to be a scalar value. If the initial simplex is computed from 'axes' method, it may be either a scalar value or a vector of values, of length n, where n is the number of variables.
- '-simplex0deltausual'** The relative delta for non-zero parameters in 'pfeffer' method.
- '-simplex0deltazero'** The absolute delta for non-zero parameters in 'pfeffer' method.
- '-rho'** The reflection coefficient. This parameter is used when the `method` element is set to 'fixed' or 'variable'.
- '-chi'** The expansion coefficient. This parameter is used when the `method` element is set to 'variable'.
- '-gamma'** The contraction coefficient. This parameter is used when the `method` element is set to 'variable'.
- '-sigma'** The shrinkage coefficient. This parameter is used when the `method` element is set to 'fixed' or 'variable'.
- '-tolsimplexizemethod'** Set to FALSE to disable the tolerance on the simplex size. If this criteria is triggered, the status of the optimization is set to 'tolsize'. When this criteria is enabled, the values of the `tolsimplexizeabsolute` and `tolsimplexizerelative` elements are used in the termination criteria. The method to compute the size is the 'sigmaplus' method.
- '-tolsimplexizeabsolute'** The absolute tolerance on the simplex size.
- '-tolsimplexizerelative'** The relative tolerance on the simplex size.
- '-tolssizedeltafvmethod'** Set to TRUE to enable the termination criteria based on the size of the simplex and the difference of function value in the simplex. If this criteria is triggered, the status of the optimization is set to 'tolssizedeltafv'. This termination criteria uses the values of the `tolsimplexizeabsolute` and `toldeltafv` elements.option
- '-toldeltafv'** The absolute tolerance on the difference between the highest and the lowest function values.
- '-tolvarianceflag'** Set to TRUE to enable the termination criteria based on the variance of the function value. If this criteria is triggered, the status of the optimization is set to 'tolvariance'. This criteria is suggested by Nelder and Mead.
- '-tolabsolutevariance'** The absolute tolerance on the variance of the function values of the simplex.
- '-tolrelativevariance'** The relative tolerance on the variance of the function values of the simplex.
- '-kelleystagnationflag'** Set to TRUE to enable the termination criteria using Kelley's stagnation detection, based on sufficient decrease condition. If this criteria is triggered, the status of the optimization is set to 'kelleystagnation'.
- '-kelleynormalizationflag'** Set to FALSE to disable the normalization of the alpha coefficient in Kelley's stagnation detection, i.e. use the value of the `kelleystagnationalpha0` element as is. Default value is TRUE, i.e. the simplex gradient of the initial simplex is takeoptionn into account in the stagnation detection.
- '-kelleystagnationalpha0'** The parameter used in Kelley's stagnation detection.

- 'restartflag'** Set to TRUE to enable the automatic restart of the algorithm.
- 'restartdetection'** The method to detect if the automatic restart must be performed. The following methods are available:
 - 'oneill'** The factorial local optimality test by O'Neill is used. If the test finds a local point which is better than the computed optimum, a restart is performed.
 - 'kelley'** The sufficient decrease condition by O'Neill is used. If the test finds that the status of the optimization is 'kelleystagnation', a restart is performed. This status may be generated if the -kelleystagnationflag option is set to TRUE.
- 'restartmax'** The maximum number of restarts, when automatic restart is enabled via the -restartflag option.
- 'restarteps'** The absolute epsilon value used to check for optimality in the factorial O'Neill restart detection.
- 'restartstep'** The absolute step length used to check for optimality in the factorial O'Neill restart detection.
- 'restartsimplexmethod'** The method to compute the initial simplex after a restart. The following methods are available.
 - 'given'** The coordinates associated with the `coords0` element are used to compute the initial simplex, with arbitrary number of vertices. This allow the user to setup the initial simplex by a specific method which is not provided by the current package (for example with a simplex computed from a design of experiments). This allows also to configure the initial simplex so that a specific behaviour of the algorithm is to be reproduced (for example the Mc Kinnon test case). The given matrix is expected to have nbve rows and n columns, where n is the dimension of the problem and nbve is the number of vertices.
 - 'axes'** The simplex is computed from the coordinate axes and the length associated with the -simplex0length option.
 - 'spendley'** The simplex is computed so that it is regular with the length associated with the -simplex0length option (i.e. all the edges have the same length).
 - 'pfeffer'** The simplex is computed from an heuristic, in the neighborhood of the initial guess. This initial simplex depends on the -simplex0deltausual and -simplex0deltazero.
 - 'randbounds'** The simplex is computed from the bounds and a random number. This option is available only if bounds are available: if bounds are not available, an error is generated. This method is usually associated with Box's algorithm. The number of vertices in the simplex is taken from the -boxnbpoints option.
 - 'oriented'** The simplex is computed so that it is oriented, as suggested by Kelley.
- 'scalingsimplex0'** The algorithm used to scale the initial simplex into the nonlinear constraints. The following two algorithms are provided:
 - 'tox0'** scales the vertices toward the initial guess.
 - 'tocentroid'** scales the vertices toward the centroid, as recommended by Box.

If the centroid happens to be unfeasible, because the constraints are not convex, the scaling of the initial simplex toward the centroid may fail. Since the initial guess is always feasible, scaling toward the initial guess cannot fail.
- 'boxnbpoints'** The number of points in the initial simplex, when the -simplex0method is set to 'randbounds'. The value of this option is also use to update the simplex when a restart is

performed and the -restartsimplexmethod option is set to 'randbounds'. The default value is so that the number of points is twice the number of variables of the problem.

- '-boxineqscaling' The scaling coefficient used to scale the trial point for function improvement or into the constraints of Box's algorithm.
- '-guinalphamin' The minimum value of alpha when scaling the vertices of the simplex into nonlinear constraints in Box's algorithm.
- '-boxreflect' The reflection factor in Box's algorithm.
- '-boxtermination' Set to TRUE to enable Box's termination criteria.
- '-boxtolf' The absolute tolerance on difference of function values in the simplex, suggested by Box. This tolerance is used if the -boxtermination element is set to TRUE.
- '-boxnbmatch' The number of consecutive match of Box's termination criteria.
- '-boxboundsalpha' The parameter used to project the vertices into the bounds in Box's algorithm.
- '-mymethod' A user-derived simplex algorithm. See `vignette('neldermead', package='neldermead')` for details.
- '-myterminate' A user-defined terminate function. See `vignette('neldermead', package='neldermead')` for details.
- '-myterminateflag' Set to TRUE to enable the user-defined terminate function.

Value

An updated neldermead object.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

`neldermead`

`neldermead.destroy` *Erase a neldermead object.*

Description

`neldermead.destroy` calls `optimbase.destroy` and `optimsimplex.destroy` to erase the content of `this$optbase` and `this$simplex0`.

Usage

```
neldermead.destroy(this = NULL)
```

Arguments

this A neldermead object.

Value

Return an updated neldermead object.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

`optimbase.destroy`, `optimsimplex.destroy`

Get functions

Get the value for the given key

Description

Get the value for the given key in a neldermead object.

Usage

```
neldermead.get(this = NULL, key = NULL)
neldermead.cget(this = NULL, key = NULL)
```

Arguments

this A neldermead object.

key The name of the key to query. The list of available keys for query with `neldermead.get` is: '-historysimplex', '-simplexopt', '-simplex0', and '-restartnb'. If **key** is different, the query is delegated to `optimbase.get`. The list of available keys for query with `neldermead.cget` is: '-method', '-coords0', '-simplex0method', '-simplex0length', '-simplex0deltausual', '-simplex0deltazero', '-rho', '-chi', '-gamma', '-sigma', '-tolsimplexeabsolute', '-tolsimplexizerelative', '-tolsimplexizemethod', '-toldeltafv', '-tolssizedeltafvmethod', '-restartmax', '-restarteps', '-restartstep', '-kelleystagnationflag', '-kelleynormalizationflag', '-kelleystagnationalpha0', '-restartflag', '-restartdetection', '-restartsimplexmethod', '-checkcostfunction', '-boxnbpoints', '-boxineqscaling', '-scalingsimplex0', '-guinalphamin', '-boxtermination', '-boxtolf', '-boxnbmatch', '-boxreflect', '-mymethod', '-myterminate', '-myterminateflag', '-tolvarianceflag', '-tolabsolutevariance', '-tolrelativevariance', and '-greedy'. If **key** is different, the query is delegated to `optimbase.cget`.

Value

Return the value of the list element **key**, or an error message if **key** does not exist.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

`neldermead.configure`, `optimbase.cget`, `optimbase.get`

`neldermead`

S3 neldermead object

Description

These functions support the S3 class 'neldermead' and are intended to either create objects of this class or check if an object is of this class.

Usage

```
neldermead(optbase, method, simplex0, simplex0method,
           simplex0length, simplexsize0, simplexopt, historysimplex, coords0, rho, chi,
           gamma, sigma, tolfstdeviation, tolfsdeviationmethod, tolsimplexizeabsolute,
           tolsimplexizerelative, tolsimplexizemethod, toldeltafv, tolssizedeltafvmethod,
           simplex0deltausual, simplex0deltazero, restartsimplexmethod, restartmax,
           restarteps, restartstep, restartnb, restartflag, restartdetection,
           kelleystagnationflag, kelleynormalizationflag, kelleystagnationalpha0,
           kelleyalpha, startupflag, boxnbpoints, boxnbpointseff, boxineqscaling,
           checkcostfunction, scalingsimplex0, guinalphamin, boxboundsalpha,
           boxtermination, boxtolf, boxnbmatch, boxkount, boxreflect, tolvarianceflag,
           tolabsolutevariance, tolrelativevariance, variancesimplex0, mymethod,
           myterminate, myterminateflag, greedy, output, exitflag)

## S3 method for class 'neldermead'
print(x,verbose,...)

## S3 method for class 'neldermead'
summary(object,showhistory,...)

## S3 method for class 'neldermead'
is(x=NULL)
```

Arguments

optbase An object of class 'optimbase', i.e. a list created by `optimbase()` and containing the following elements:
verbose The verbose option, controlling the amount of messages.

x0 The initial guess.
fx0 The value of the function for the initial guess.
xopt The optimum parameter.
fopt The optimum function value.
tolfunabsolute The absolute tolerance on function value.
tolfunrelative The relative tolerance on function value.
tolfunmethod Logical flag for the tolerance on function value in the termination criteria. This criteria is suitable for functions which minimum is associated with a function value equal to 0.
tolxabsolute The absolute tolerance on x.
tolxrelative The relative tolerance on x.
tolxmethod Possible values: FALSE, TRUE.
funevals The number of function evaluations.
maxfunevals The maximum number of function evaluations.
maxiter The maximum number of iterations.
iterations The number of iterations.
fun The cost function.
status The status of the optimization.
historyfopt The vector to store the history for fopt. The values of the cost function will be stored at each iteration in a new element, so the length of **historyfopt** at the end of the optimization should be the number of iterations.
historyxopt The list to store the history for xopt. The vectors of estimates will be stored on separated levels of the list, so the length of **historyfopt** at the end of the optimization should be the number of iterations.
verbosetermination The verbose option for termination criteria.
outputcommand The command called back for output.
outputcommandarg The outputcommand argument is initialized as a string. If the user configure this element, it is expected that a matrix of values or a list is passed so that the argument is appended to the name of the function.
numberofvariables The number of variables to optimize.
storehistory The flag which enables/disables the storing of the history.
costfargument The costf argument is initialized as a string. If the user configure this element, it is expected that a matrix of values or a list is passed so that the argument is appended to the name of the function.
boundsmin Minimum bounds for the parameters.
boundsmax Maximum bounds for the parameters.
nbineqconst The number of nonlinear inequality constraints.
logfile The name of the log file.
logfilehandle The handle for the log file.
logstartup Set to TRUE when the logging is started up.
withderivatives Set to TRUE when the method uses derivatives.
method The name of the algorithm to use.

simplex0	An object of class 'simplex', i.e. a list created by <code>optim simplex()</code> , and containing the following elements:
verbose	The verbose option, controlling the amount of messages.
x	The coordinates of the vertices, with size nbve x n.
n	The dimension of the space.
fv	The function values, with size nbve x 1.
nbve	The number of vertices.
simplex0method	The method to use to compute the initial simplex.
simplex0length	The length to use when the initial simplex is computed with the 'axes' or 'spendley' methods.
rho	The reflection coefficient. This parameter is used when the <code>method</code> element is set to 'fixed' or 'variable'.
chi	The expansion coefficient. This parameter is used when the <code>method</code> element is set to 'variable'.
gamma	The contraction coefficient. This parameter is used when the <code>method</code> element is set to 'variable'.
sigma	The shrinkage coefficient. This parameter is used when the <code>method</code> element is set to 'fixed' or 'variable'.
tolfstdeviation	The tolerance for the standard deviation.
tolfstdeviationmethod	Set to FALSE.
tolsimplexizeabsolute	The absolute tolerance on the simplex size.
tolsimplexizerelative	The relative tolerance on the simplex size.
tolsimplexizemethod	Logical flag to enable/disable the tolerance on the simplex size. When this criteria is enabled, the values of the <code>tolsimplexizeabsolute</code> and <code>tolsimplexizerelative</code> elements are used in the termination criteria. The method to compute the size is the 'sigmaplus' method.
simplexsize0	Initial size of the simplex, for the tolerance on the simplex size.
toldeltafv	The absolute tolerance on the difference between the highest and the lowest function values.
tolssizedeltafvmethod	Logical flag to enable/disable the termination criteria based on the size of the simplex and the difference of function value in the simplex. If this criteria is triggered, the status of the optimization is set to 'tolssizedeltafv'. This termination criteria uses the values of the <code>tolsimplexizeabsolute</code> and <code>toldeltafv</code> elements. This criteria is identical to Scilab's <code>fminsearch</code> .
historysimplex	The list to store the history for simplex. The simplex will be stored on a new level of the list at each iteration, so the length of <code>historyfopt</code> at the end of the optimization should be the number of iterations.

coords0	The coordinates of the vertices of the initial simplex. If the simplex0method element is set to 'given', these coordinates are used to compute the initial simplex. This matrix is expected to have shape nbve x n where nbve is the number of vertices and n is the number of variables.
simplex0deltausual	The relative delta for non-zero parameters in 'pfeffer' method.
simplex0deltazero	The absolute delta for non-zero parameters in 'pfeffer' method.
simplexopt	The optimum simplex, after one optimization process.
restartsimplexmetho	The method to compute the initial simplex after a restart.
restartmax	The maximum number of restarts, when automatic restart is enabled via the restartflag element.
restarteps	The absolute epsilon value used to check for optimality in the factorial O'Neill restart detection.
restartstep	The absolute step length used to check for optimality in the factorial O'Neill restart detection.
kelleystagnationflag	Logical flag to enable/disable the termination criteria using Kelley's stagnation detection, based on sufficient decrease condition. If this criteria is triggered, the status of the optimization is set to 'kelleystagnation'.,
kelleynormalizationflag	Logical flag to enable/disable the normalization of the alpha coefficient in Kelley's stagnation detection, i.e. use the value of the kelleystagnationalpha0 element as is.
kelleystagnationalpha0	The parameter used in Kelley's stagnation detection.
kelleyalpha	The current value of Kelley's alpha, after normalization, if required.
restartnb	Number of restarts performed.
restartflag	Logical flag to enable/disable the automatic restart of the algorithm.
restartdetection	The method to detect if the automatic restart must be performed.
startupflag	Set to TRUE when the startup has been performed.
boxnbpoints	The number of points in the initial simplex, when the simplex0method is set to 'randbounds'. The value of this element is also use to update the simplex when a restart is performed and the restartsimplexmetho element is set to 'randbounds'. The default value is so that the number of points is twice the number of variables of the problem.
boxnbpointseff	The effective number of points required in the simplex for Box's algorithm.
boxineqscaling	The scaling coefficient used to scale the trial point for function improvement or into the constraints of Box's algorithm.
checkcostfunction	Logical flag to enable/disable the checking of the connection of the cost function.

scalingsimplex0	
	The algorithm used to scale the initial simplex into the nonlinear constraints. The following two algorithms are provided:
'tox0'	scales the vertices toward the initial guess.
'tocentroid'	scales the vertices toward the centroid, as recommended by Box. If the centroid happens to be unfeasible, because the constraints are not convex, the scaling of the initial simplex toward the centroid may fail. Since the initial guess is always feasible, scaling toward the initial guess cannot fail.
guinalphamin	The minimum value of alpha when scaling the vertices of the simplex into nonlinear constraints in Box's algorithm.
boxboundsalpha	The parameter used to project the vertices into the bounds in Box's algorithm.
boxtermination	Logical flag to enable/disable Box's termination criteria.
boxtolf	The absolute tolerance on difference of function values in the simplex, suggested by Box. This tolerance is used if the boxtermination element is set to TRUE.
boxnbmatch	The number of consecutive match of Box's termination criteria.
boxkount	Current number of consecutive match.
boxreflect	The reflection factor in Box's algorithm.
tolvarianceflag	Logical flag to enable/disable the termination criteria based on the variance of the function value. If this criteria is triggered, the status of the optimization is set to 'tolvariance'. This criteria is suggested by Nelder and Mead.
tolabsolutevariance	The absolute tolerance on the variance of the function values of the simplex.
tolrelativevariance	The relative tolerance on the variance of the function values of the simplex.
variancesimplex0	
	Relative tolerance on variance.
mymethod	A user-defined simplex algorithm.
myterminate	A user-defined terminate function.
myterminateflag	Logical flag to enable/disable the user-defined terminate function.
greedy	Logical flag to enable/disable greedy Nelder-Mead.
output	The command to call back for user-defined output of specialized function.
exitflag	Logical flag to enable/disable the user-defined output of specialized function.
x	An object of class 'neldermead'.
verbose	A logical flag, controlling the amount of data printed.
...	optional arguments to 'print' or 'plot' methods.
object	An object of class 'neldermead'.
showhistory	Optional logical flag, to define whether optimization history must be summarized or not.

Value

The **neldermead** function returns a new object of class 'neldermead', with the following default content:

optbase An object of class 'optimbase' with the following default content:

verbose Default is FALSE.
x0 Default is NULL.
fx0 Default is NULL.
xopt Default is 0.
fopt Default is 0.
tolfunabsolute Default is 0.
tolfunrelative Default is .Machine\$double.eps.
tolfunmethod Default is FALSE.
tolxabsolute Default is 0.
tolxrelative Default is .Machine\$double.eps.
tolxmethod Default is TRUE.
funevals Default is 0.
maxfunevals Default is 100.
maxiter Default is 100.
iterations Default is 0.
fun Default is ".
status Default is ".
historyfopt Default is NULL.
historyxopt Default is NULL.
verbosetermination Default is FALSE.
outputcommand Default is ".
outputcommandarg Default is ". If the user configures this element, it is expected to be an object of class 'optimbase.outputargs' or will be coerced to an object of class 'optimbase.outputargs'.
numberofvariables Default is 0.
storehistory Default is FALSE.
costfargument Default is ". If the user configures this element, it is expected to be an object of class 'optimbase.functionargs' or will be coerced to an object of class 'optimbase.functionargs'.
boundsmin Default is NULL.
boundsmax Default is NULL.
nbineqconst Default is 0.
logfile Default is ".
logfilehandle Default is 0.
logstartup Default is FALSE.
withderivatives Default is FALSE.
method Default is 'variable'.
simplex0 Default is an object of class 'simplex', with the following content:

verbose Default is 0.
x Default is NULL.
n Default is 0.
fv Default is NULL.
nbve Default is 0.
simplex0method Default is 'axes'.
simplex0length Default is 1.
rho Default is 1.
chi Default is 2.
gamma Default is 0.5.
sigma Default is 0.5.
tolfstdeviation Default is 0.
tolfstdeviationmethod Default is FALSE.
tolsimplexizeabsolute Default is 0.
tolsimplexizerelative Default is .Machine\$double.eps.
tolsimplexizemethod Default is FALSE.
simplexsize0 Default is 0.
toldeltafv Default is .Machine\$double.eps.
tolssizedeltafvmethod Default is FALSE.
historysimplex Default is NULL.
coords0 Default is NULL.
simplex0deltausual Default is 0.05.
simplex0deltazero Default is 0.0075.
simplexopt Default is NULL.
restartsimplexmethod Default is 'oriented'.
restartmax Default is 3.
restarteps Default is .Machine\$double.eps.
restartstep Default is 1.
kelleystagnationflag Default is FALSE.,
kelleynormalizationflag Default is TRUE, i.e. the simplex gradient of the initial simplex is taken into account in the stagnation detection.
kelleystagnationalpha0 Default is 1.e-4.
kelleyalpha Default is 1.e-4.
restartnb Default is 0.
restartflag Default is FALSE.
restartdetection Default is 'oneill'.
startupflag Default is FALSE.
boxnbpoints Default is '2n'.

boxnbpointseff Default is 0.
boxineqscaling Default is 0.
checkcostfunction Default is TRUE.
scalingsimplex0 Default is 'tox0'.
guinalphamin Default is 1.e-6.
boxtermination Default is FALSE.
boxtolf Default is 1.e-5.
boxnbmatch Default is 5.
boxkount Default is 0.
boxreflect Default is 1.3.
tolvarianceflag Default is FALSE.
tolabsolutevariance Default is 0.
tolrelativevariance Default is .Machine\$double.eps.
variancesimplex0 Default is .Machine\$double.eps.
mymethod Default is NULL.
myterminate Default is NULL.
myterminateflag Default is FALSE.
greedy Default is FALSE.
output Default is list().
exitflag Default is FALSE.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

optimbase, **optimsimplex**

neldermead.restart *Restart neldermead search.*

Description

Update the simplex with **neldermead.updatesimp** and restart the search with **neldermead.search**.

Usage

```
neldermead.restart(this = NULL)
```

Arguments

this A neldermead object.

Value

Returns an updated neldermead object.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

`neldermead.updatesimp`, `neldermead.search`,

`neldermead.search` *Starts the optimization*

Description

Performs the optimization associated with the method associated with the `method` element of the neldermead object and find the optimum. If the `restartflag` element is enabled, automatic restarts are performed, based on the `restartdetection` element.

Usage

`neldermead.search(this = NULL)`

Arguments

this A neldermead object.

Value

Return an updated neldermead object.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

`fminsearch`, `neldermead`, `neldermead.configure`,

Secondary search functions

Secondary functions for neldermead.search

Description

Utility functions for `neldermead.serch` and dependent functions.

Usage

```
neldermead.startup(this = NULL)
neldermead.log(this = NULL, msg = NULL)
neldermead.scaletox0(this = NULL, simplex0 = NULL)
neldermead.scaletocenter(this = NULL, simplex0 = NULL, x0 = NULL)
neldermead.termstartup(this = NULL)
neldermead.outputcmd(this = NULL, state = NULL, simplex = NULL, step = NULL)
neldermead.autorestart(this = NULL)
neldermead.istorestart(this = NULL)
neldermead.isroneill(this = NULL)
neldermead.isrkelly(this = this)
neldermead.updatesimp(this = NULL)
scaleinconstraints(this = NULL, x = NULL, xref = NULL)
neldermead.costf(x = NULL, this = NULL)
```

Arguments

<code>this</code>	A neldermead object.
<code>msg</code>	A character string.
<code>simplex0</code>	The initial simplex object.
<code>x0</code>	A column matrix of initial parameters.
<code>state</code>	The state of the algorithm, either 'init', 'done' or 'iter'.
<code>simplex</code>	The current simplex object.
<code>step</code>	The type of step performed during the iteration: 'init', 'done', 'reflection', 'expansion', 'insidecontraction', 'outsidecontraction', 'reflectionnext' or 'shrink'.
<code>x</code>	The point estimate to scale.
<code>xref</code>	The reference point estimate.

Details

- `neldermead.startup` Startup the algorithm. Compute the initial simplex, depending on the content of the `simplex0method` element of the neldermead object ('given', 'axes', 'spendley', 'pfeffer' or 'randbounds').
- `neldermead.log` Print a message to the log file using `optimbase.log`.
- `neldermead.scaletox0` Scale the simplex into the nonlinear inequality constraints, if any. Scale toward `x0`, which is feasible.

neldermead.scaletocenter Scale the simplex into the nonlinear inequality constraints, if any.
 Scale to the centroid of the points which satisfy the constraints. This is Box's method for scaling. It is unsure, since the centroid of the points which satisfy the constraints may not be feasible.

neldermead.termstartup Initialize Kelley's stagnation detection system when normalization is required, by computing kelleyalpha. If the simplex gradient is zero, then use alpha0 as alpha.

neldermead.outputcmd Call the array of user-defined output functions

neldermead.autorestart Perform an optimization with automatic restart. The loop processes for $i = 1$ to `restartmax + 1`. This is because a RE-start is performed after one simulation has been performed, hence the 'RE'.

neldermead.istorestart Determine if the optimization is to restart using `neldermead.isroneill` or `neldermead.isrkelly` depending on the content of the `restartdetection` element.

neldermead.isroneill Determine if the optimization is to restart. Use O'Neill method as a criteria for restart. It is an axis-by-axis search for optimality.

neldermead.isrkelly Determine if the optimization is to restart. Use `kelleystagnation` as a criteria for restart.

neldermead.updatesimp Update the initial simplex `simplex0` for a restart.

scaleinconstraints Given a point reference to scale and a reference point which satisfies the constraints, scale the point towards the reference point estimate until it satisfies all the constraints.

neldermead.costf Call the cost function and return the value. This function is given to the simplex function class as a callback. Input/Output arguments are swapped w.r.t. `optimbase.function`, so that it matches the requirements of simplex methods.

Value

neldermead.startup Return an updated neldermead object `this`.

neldermead.log Return the neldermead object `this`.

neldermead.scaletox0 Return an updated simplex.

neldermead.scaletocenter Return an updated simplex.

neldermead.termstartup Return an updated neldermead object `this`.

neldermead.outputcmd Do not return any data, but execute the output function(s).

neldermead.autorestart Return an updated neldermead object `this`.

neldermead.istorestart Return a list with the following elements:

- this** The input neldermead object.
- istorestart** Set to TRUE if the optimization is to restart, to FALSE otherwise.

neldermead.isroneill Return a list with the following elements:

- this** The input neldermead object.
- istorestart** Set to TRUE if the optimization is to restart, to FALSE otherwise.

neldermead.isrkelly Return a list with the following elements:

- this** The input neldermead object.

istorestart Set to TRUE if the optimization is to restart, to FALSE otherwise.
neldermead.updatesimp Return an updated neldermead object **this**.
scaleinconstraints Return a list with the following elements:
this The updated neldermead object.
isscaled TRUE if the procedure has succeeded before **boxbnlloops**, FALSE if it has failed.
p The scaled parameters.
neldermead.costf Return a list with the following elements:
f The value of the cost function.
this The updated neldermead object.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
 Author of R adaptation: Sébastien Bihorel (<sb.pmlab@gmail.com>)

optimget

Queries an optimization option list

Description

This function allows to make queries on an existing optimization option list. This list must have been created and updated by the **optimset** function. The **optimget** allows to retrieve the value associated with a given key.

Usage

```
optimget(options = NULL, key = NULL, value = NULL)
```

Arguments

options	A list created or modified by optimset .
key	A single character string, which should be the name of the field in options to query (case insensitive).
value	A default value.

Details

key is matched against the field names of **options** using **grep** and a case-insensitive regular expression. If **key** is not found in **options**, the function returns NULL. If several matches are found, **optimget** is stopped.

Value

Return **options\$key** if **key** is found in **options**. Return **value**, otherwise.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

`optimset`

Examples

```
opt <- optimset(method='fminsearch')
optimget(opt,'Display')
optimget(opt,'abc','!@')
```

`optimset.method`

Default set of optimization options

Description

This function returns a default set of optimization options for defined 'methods'; `optimset.method` is called by `optimset` when a `method` was provided as input. Currently, the only valid `method` is 'fminsearch'.

Usage

```
optimset.method(method = NULL)
```

Arguments

`method` A character string.

Value

Returns a list with the following fields: `Display`, `FunValCheck`, `MaxFunEvals`, `MaxIter`, `OutputFcn`, `PlotFcns`, `TolFun`, and `TolX`.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

`optimset`

Examples

```
optimset.method('fminsearch')
## Not run: optimset.method('abc')
```

optimset

Configures and returns an optimization data structure.

Description

This function creates or updates a list which can be used to modify the behaviour of optimization methods. The goal of this function is to manage the **options** list with a set of fields (for example, 'MaxFunEvals', 'MaxIter', etc...). The user can create a new list with empty fields or create a new structure with default fields which correspond to a particular algorithm. The user can also configure each field and set it to a particular value. Finally, the user passes the list to an optimization function so that the algorithm uses the options configured by the user.

Usage

```
optimset(method = NULL, ...)
```

Arguments

method	If provided, the method calls the optimset . method function. If the content of method is recognized, a default set of options are returned. The only current recognized character strings are 'fminsearch' and 'fminbnd'.
...	Additional arguments which would be included in the options output if the method argument is not used. See Details.

Details

Most optimization algorithms require many algorithmic parameters such as the number of iterations or the number of function evaluations. If these parameters are given to the optimization function as input parameters, this forces both the user and the developer to manage many input parameters. The goal of the **optimset** function is to simplify the management of input arguments, by gathering all the parameters into a single list.

While the current implementation of the **optimset** function only supports the **fminsearch** and **fminbnd** function, it is designed to be extended to as many optimization function as required. Because all optimization algorithms do not require the same parameters, the data structure aims at remaining flexible. But, most of the time, most parameters are the same from algorithm to algorithm, for example, the tolerance parameters which drive the termination criteria are often the same, even if the termination criteria itself is not the same.

Optimization parameters that are returned by the **optimset** function and that can be defined in ... are the following:

Display The verbose level. The default value is 'notify'. The following is a list of available verbose levels.

'off' The algorithm displays no message at all.

'notify' The algorithm displays message if the termination criteria is not reached at the end of the optimization. This may happen if the maximum number or iterations of the maximum number of function evaluations is reached and warns the user of a convergence problem.

'final' The algorithm displays a message at the end of the optimization, showing the number of iterations, the number of function evaluations and the status of the optimization. This option includes the messages generated by the 'notify' option i.e. warns in case of a convergence problem.

'iter' The algorithm displays a one-line message at each iteration. This option includes the messages generated by the 'notify' option i.e. warns in case of a convergence problem. It also includes the message generated by the 'final' option.

FunValCheck A logical flag to enable the checking of function values.

MaxFunEvals The maximum number of evaluations of the cost function.

MaxIter The maximum number of iterations.

OutputFcn A function which is called at each iteration to print out intermediate state of the optimization algorithm (for example into a log file).

PlotFcns A function which is called at each iteration to plot the intermediate state of the optimization algorithm (for example into a 2D graphic).

TolFun The absolute tolerance on function value.

TolX The absolute tolerance on the variable x.

nbMatch Specific to Box method: the number of consecutive times the TolFun criteria must be met to terminate the optimization.

boundsAlpha Specific to Box method: the parameter used to project the vertices into the bounds in Box's algorithm

boxScaling Specific to Box method: the scaling coefficient used to scale the trial point for function improvement or into the constraints of Box's algorithm

alphaMin Specific to Box method: the minimum value of alpha when scaling the vertices of the simplex into nonlinear constraints in Box's algorithm

Output and plot functions The 'OutputFcn' and 'PlotFcns' options accept as argument a function (or a list of functions). In the client optimization algorithm, this output or plot function is called back once per iteration. It can be used by the user to display a message in the console, write into a file, etc... The output or plot function is expected to have the following definition:

```
myfun <- function(x, optimValues, state)
```

where the input parameters are:

x The current point estimate.

optimValues A list which contains the following fields:

funcCount The number of function evaluations.

fval The best function value.

iteration The current iteration number.

procedure The type of step performed. This string depends on the specific algorithm (see **fminsearch** for details).

state the state of the algorithm. The following states are available:

'init' when the algorithm is initializing,

'iter' when the algorithm is performing iterations,

'done' when the algorithm is terminated.

Value

Return a list with the following fields: Display, FunValCheck, MaxFunEvals, MaxIter, OutputFcn, PlotFcns, TolFun, TolX, nbMatch, boundsAlpha, boxScaling, and alphaMin.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

`optimset.method`, `fminsearch`, `fminbnd`

Examples

```
optimset()
optimset(Display='iter')
optimset(method='fminbnd')
```

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11.5 LANGUAGE

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Version 2.0 dated 2006-09-05.