

rebmix: Finite Mixture Modeling, Clustering & Classification

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Abstract

The **rebmix** package provides R functions for random univariate and multivariate finite mixture model generation, estimation, clustering and classification. Variables can be continuous, discrete, independent or dependent and may follow normal, lognormal, Weibull, gamma, binomial, Poisson or Dirac parametric families.

1 Introduction

To cite the REBMIX algorithm please refer to (Nagode and Fajdiga, 2011a,b; Nagode, 2015). For theoretical backgrounds please upload also <http://doi.org/10.5963/JA00302001>.

2 What's new in version 2.8.0

R code is extended and rewritten in S4 class system. The background C code is extended and rewritten as object-oriented C++ code, too. The package can easier be extended to other parametric families. Multivariate normal mixtures with unrestricted variance-covariance matrices are added. Clustering is added and classification is improved.

3 Examples

To illustrate the use of the REBMIX algorithm, univariate and multivariate datasets are considered. The **rebmix** is loaded and the prompt before starting new page is set to TRUE.

```
R> library("rebmix")
R> devAskNewPage(ask = TRUE)
```

3.1 Gamma datasets

Three gamma mixtures are considered (Wiper et al., 2001). The first has four well-separated components with means 2, 4, 6 and 8, respectively

$$\begin{aligned}\theta_1 &= 1/100 & \beta_1 &= 200 & n_1 &= 100 \\ \theta_2 &= 1/100 & \beta_2 &= 400 & n_2 &= 100 \\ \theta_3 &= 1/100 & \beta_3 &= 600 & n_3 &= 100 \\ \theta_4 &= 1/100 & \beta_4 &= 800 & n_4 &= 100.\end{aligned}$$

The second has equal means but different variances and weights

$$\begin{aligned}\theta_1 &= 1/27 & \beta_1 &= 9 & n_1 &= 40 \\ \theta_2 &= 1/270 & \beta_2 &= 90 & n_2 &= 360.\end{aligned}$$

The third is a mixture of a rather diffuse component with mean 6 and two lower weighted components with smaller variances and means of 2 and 10, respectively

$$\begin{aligned}\theta_1 &= 1/20 & \beta_1 &= 40 & n_1 &= 80 \\ \theta_2 &= 1 & \beta_2 &= 6 & n_2 &= 240 \\ \theta_3 &= 1/20 & \beta_3 &= 200 & n_3 &= 80.\end{aligned}$$

3.1.1 Finite mixture generation

```
R> n <- c(100, 100, 100, 100)
R> Theta <- list(pdf1 = "gamma", theta1.1 = c(1/100, 1/100, 1/100,
+      1/100), theta2.1 = c(200, 400, 600, 800))
R> gamma1 <- RNGMIX(Dataset.name = "gamma1", n = n, Theta = Theta)
R> n <- c(40, 360)
R> Theta <- list(pdf1 = "gamma", theta1.1 = c(1/27, 1/270), theta2.1 = c(9,
+      90))
R> gamma2 <- RNGMIX(Dataset.name = "gamma2", n = n, Theta = Theta)
R> n <- c(80, 240, 80)
R> Theta <- list(pdf1 = "gamma", theta1.1 = c(1/20, 1, 1/20), theta2.1 = c(40,
+      6, 200))
R> gamma3 <- RNGMIX(Dataset.name = "gamma3", n = n, Theta = Theta)
```

3.1.2 Finite mixture estimation

```
R> gamma1est <- REBMIX(Dataset = gamma1@Dataset, Preprocessing = "histogram",
+      cmax = 8, Criterion = c("AIC", "BIC"), pdf = "gamma", K = 30:80)
R> gamma2est <- REBMIX(Dataset = gamma2@Dataset, Preprocessing = "histogram",
+      cmax = 8, Criterion = "BIC", pdf = "gamma", K = 30:80)
R> gamma3est <- REBMIX(Dataset = gamma3@Dataset, Preprocessing = "histogram",
+      cmax = 8, Criterion = "BIC", pdf = "gamma", K = 30:80)
```

3.1.3 Summary and coef methods

```
R> summary(gamma2est)
```

Dataset	Preprocessing	Criterion	c	v/k	IC	logL	M
1 gamma2	histogram	BIC	2	55	-1348	689	5

Maximum logL = 689 at pos = 1.

```
R> coef(gamma3est)
```

	comp1	comp2	comp3
w	0.281	0.238	0.481
theta1.1	0.1367		
theta1.2	0.0428		
theta1.3	0.6709		
theta2.1	16.48	1	
theta2.2	235.71		
theta2.3	9.11		

3.1.4 Bootstrap methods

```
R> gamma3boot <- boot(x = gamma3est, pos = 1, Bootstrap = "p", B = 10)
R> gamma3boot
```

An object of class "REBMIX.boot"

Slot "c":

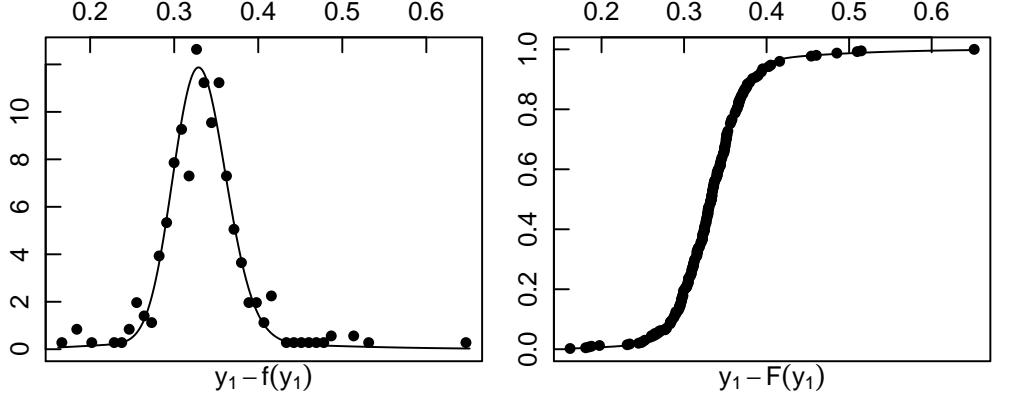
```
[1] 3 3 3 3 3 3 3 3 3 3
```

Slot "c.se":

```
[1] 0
```

Slot "c.cv":

```
R> plot(gamma2est, pos = 1, what = c("den", "dis"), ncol = 2, npts = 1000)
```



Dataset = gamma2, Preprocessing = histogram, Restraints = loose, $c_{\max} = 8$, $a_r = 0.1$, $c = 2$, $v = 55$, BIC = -1348, log L = 689.

Figure 1: Gamma 2 dataset. Empirical density (circles) and predictive gamma mixture density in black solid line.

```
[1] 0
Slot "c.mode":
[1] 3
Slot "c.prob":
[1] 1
```

```
R> summary(gamma3boot)
```

	comp1	comp2	comp3
w.cv	0.118	0.163	0.169
theta1.1.cv	0.500		
theta1.2.cv	1.033		
theta1.3.cv	0.619		
theta2.1.cv	2.028		
theta2.2.cv	0.797		
theta2.3.cv	1.378		

Mode probability = 1 at c = 3 components.

3.1.5 Plot method

3.2 Poisson dataset

Dataset consists of $n = 600$ two dimensional observations obtained by generating data points separately from each of three Poisson distributions. The component dataset sizes and parameters, which are those studied in Ma et al. (2009), are displayed below

$$\begin{aligned}\boldsymbol{\theta}_1 &= (3, 2)^T & n_1 &= 200 \\ \boldsymbol{\theta}_2 &= (9, 10)^T & n_2 &= 200 \\ \boldsymbol{\theta}_3 &= (15, 16)^T & n_3 &= 200\end{aligned}$$

For the dataset Ma et al. (2009) conduct 100 experiments by selecting different initial values of the mixing proportions. In all the cases, the adaptive gradient BYY learning algorithm leads to the correct model selection, i.e., finally allocating the correct number of Poissons for the dataset. In the meantime, it also results in an estimate for each parameter in the original or true Poisson mixture

which generated the dataset. As the dataset of Ma et al. (2009) can not exactly be reproduced, 10 datasets are generated with random seeds r_{seed} ranging from -1 to -10 .

3.2.1 Finite mixture generation

```
R> n <- c(200, 200, 200)
R> Theta <- list(pdf1 = rep("Poisson", 2), theta1.1 = c(3, 2), theta2.1 = c(NA,
+      NA), pdf2 = rep("Poisson", 2), theta1.2 = c(9, 10), theta2.2 = c(NA,
+      NA), pdf3 = rep("Poisson", 2), theta1.3 = c(15, 16), theta2.3 = c(NA,
+      NA))
R> poisson <- RNGMIX(Dataset.name = paste("Poisson_", 1:10, sep = ""),
+      n = n, Theta = Theta)
```

3.2.2 Finite mixture estimation

```
R> poissonest <- REBMIX(Dataset = poisson@Dataset, Preprocessing = "histogram",
+      cmax = 6, Criterion = "MDL5", pdf = rep("Poisson", 2), K = 1)
```

3.2.3 Summary and coef methods

```
R> summary(poissonest)
```

	Dataset	Preprocessing	Criterion	c	v/k	IC	logL	M
1	Poisson_1	histogram	MDL5	2	1	7151	-3496	5
2	Poisson_2	histogram	MDL5	3	1	7118	-3431	8
3	Poisson_3	histogram	MDL5	5	1	7242	-3397	14
4	Poisson_4	histogram	MDL5	3	1	7027	-3386	8
5	Poisson_5	histogram	MDL5	3	1	7132	-3438	8
6	Poisson_6	histogram	MDL5	3	1	7130	-3437	8
7	Poisson_7	histogram	MDL5	3	1	7179	-3461	8
8	Poisson_8	histogram	MDL5	3	1	7072	-3408	8
9	Poisson_9	histogram	MDL5	3	1	7026	-3385	8
10	Poisson_10	histogram	MDL5	2	1	7097	-3469	5

Maximum logL = -3385 at pos = 9.

```
R> coef(poissonest, pos = 9)
```

```
comp1 comp2 comp3
w 0.334 0.249 0.417
      1     2
theta1.1 2.93 2.01
theta1.2 8.25 9.31
theta1.3 14.05 15.49
      1 2
theta2.1 0 0
theta2.2 0 0
theta2.3 0 0
```

3.2.4 Plot method

3.2.5 Clustering

```
R> plot(poissonest, pos = 7, what = c("dens", "marg", "IC", "D",
+ "logL"), nrow = 2, ncol = 3, npts = 1000)
```

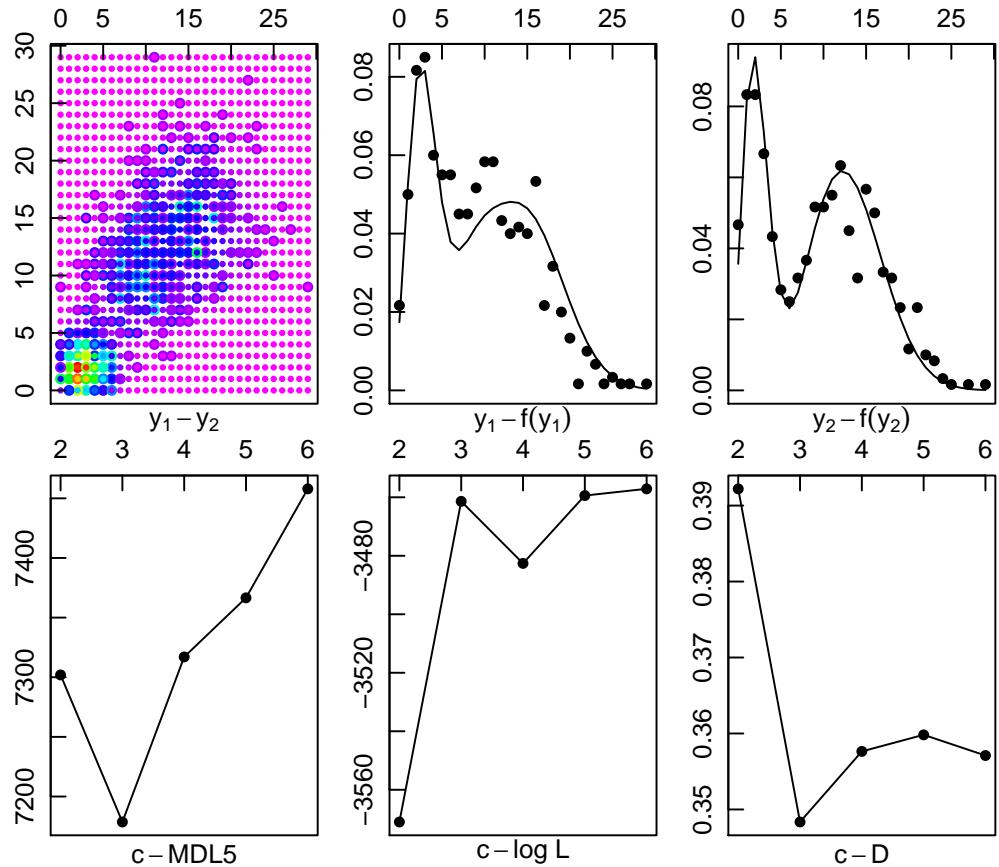


Figure 2: Poisson dataset. Empirical densities (coloured large circles), predictive multivariate Poisson-Poisson mixture density (coloured small circles), empirical densities (circles), predictive univariate marginal Poisson mixture densities and progress charts (solid line).

```
R> poissonclu <- RCLRMIX(x = poissonest, pos = 9, Zt = poisson@Zt)
R> plot(poissonclu)
```

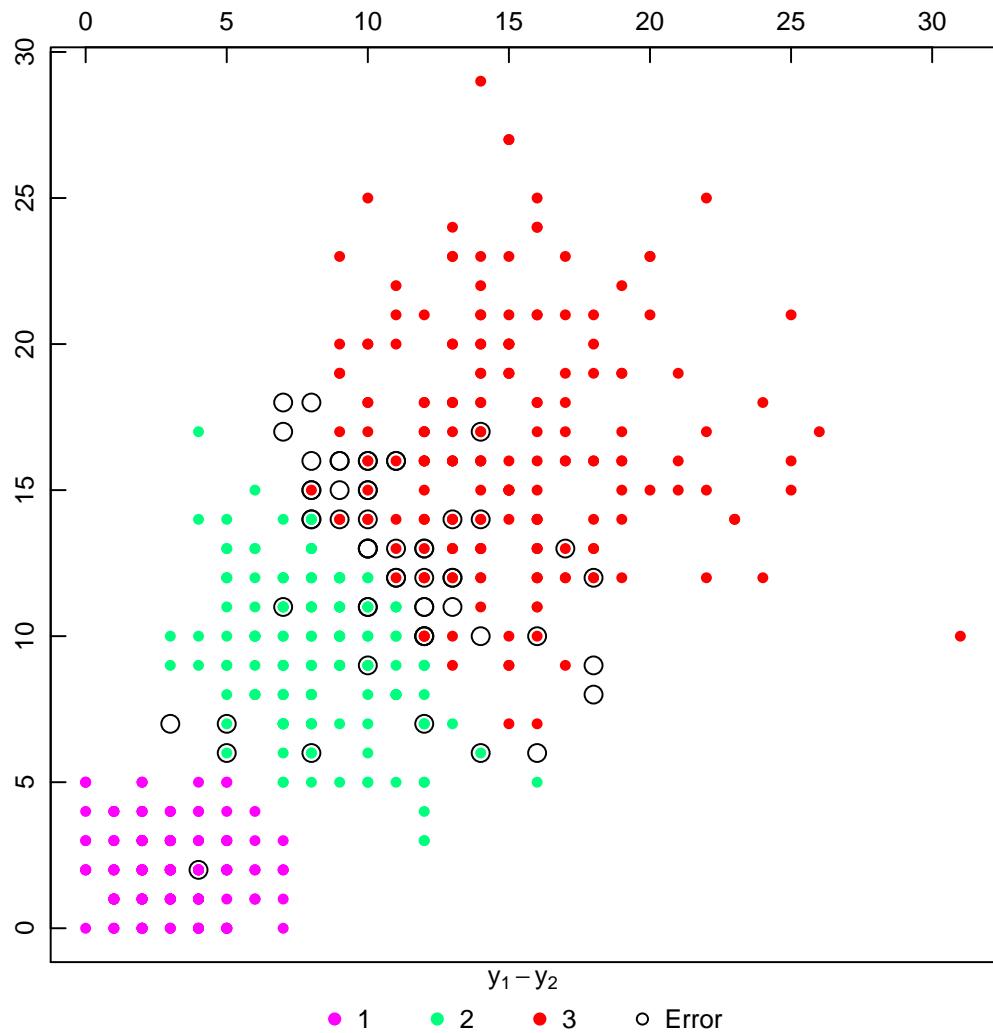


Figure 3: Poisson dataset. Predictive cluster membership (coloured circles), error (large circles).

3.3 Multivariate normal wreath dataset

A `wreath` dataset (Fraley et al., 2005) consist of 1000 observations drawn from a 14-component normal mixture in which the covariances of the components have the same size and shape but differ in orientation.

3.3.1 Finite mixture estimation

```
R> data("wreath", package = "mclust")
R> n <- nrow(wreath)
R> K <- c(as.integer(1 + log2(sum(n))), as.integer(2 * sum(n)^0.5))
R> wreathest <- REBMIX(model = "REBMVNORM", Dataset = list(as.data.frame(wreath)),
+   Preprocessing = "histogram", cmax = 20, Criterion = "BIC",
+   pdf = rep("normal", ncol(wreath)), K = K[1]:K[2])
```

3.3.2 Summary and coef methods

```
R> summary(wreathest)
```

	Dataset	Preprocessing	Criterion	c	v/k	IC	logL	M
1	dataset1	histogram	BIC	14	61	11228	-5327	83
							Maximum logL = -5327 at pos = 1.	

```
R> coef(wreathest)
```

	comp1	comp2	comp3	comp4	comp5	comp6	comp7	comp8	comp9	comp10	comp11	comp12	comp13	comp14
w	0.077	0.066	0.07	0.074	0.068	0.069	0.074	0.081	0.082	0.06	0.063	0.072		
w	0.078	0.066												
	1	2												
theta1.1	10.31	13.2137												
theta1.2	-3.67	-15.8101												
theta1.3	-14.67	7.0417												
theta1.4	-11.19	-0.0343												
theta1.5	-7.15	-8.3135												
theta1.6	2.38	-10.7039												
theta1.7	9.75	4.7284												
theta1.8	16.41	0.0472												
theta1.9	10.50	-12.8162												
theta1.10	-3.67	15.9780												
theta1.11	-6.73	8.9179												
theta1.12	2.25	11.1619												
theta1.13	9.62	-4.9869												
theta1.14	-14.95	-6.6997												
	1-1	1-2	2-1	2-2										
theta2.1	0.442	0.504	0.504	1.463										
theta2.2	0.566	-0.524	-0.524	1.691										
theta2.3	0.947	-0.566	-0.566	1.420										
theta2.4	1.106	0.457	0.457	0.812										
theta2.5	1.576	0.424	0.424	0.469										
theta2.6	1.344	0.236	0.236	0.537										
theta2.7	1.484	-0.294	-0.294	0.559										
theta2.8	0.979	-0.434	-0.434	0.847										
theta2.9	0.755	-0.206	-0.206	1.094										
theta2.10	1.253	0.358	0.358	0.752										

```
R> plot(wreathest)
```

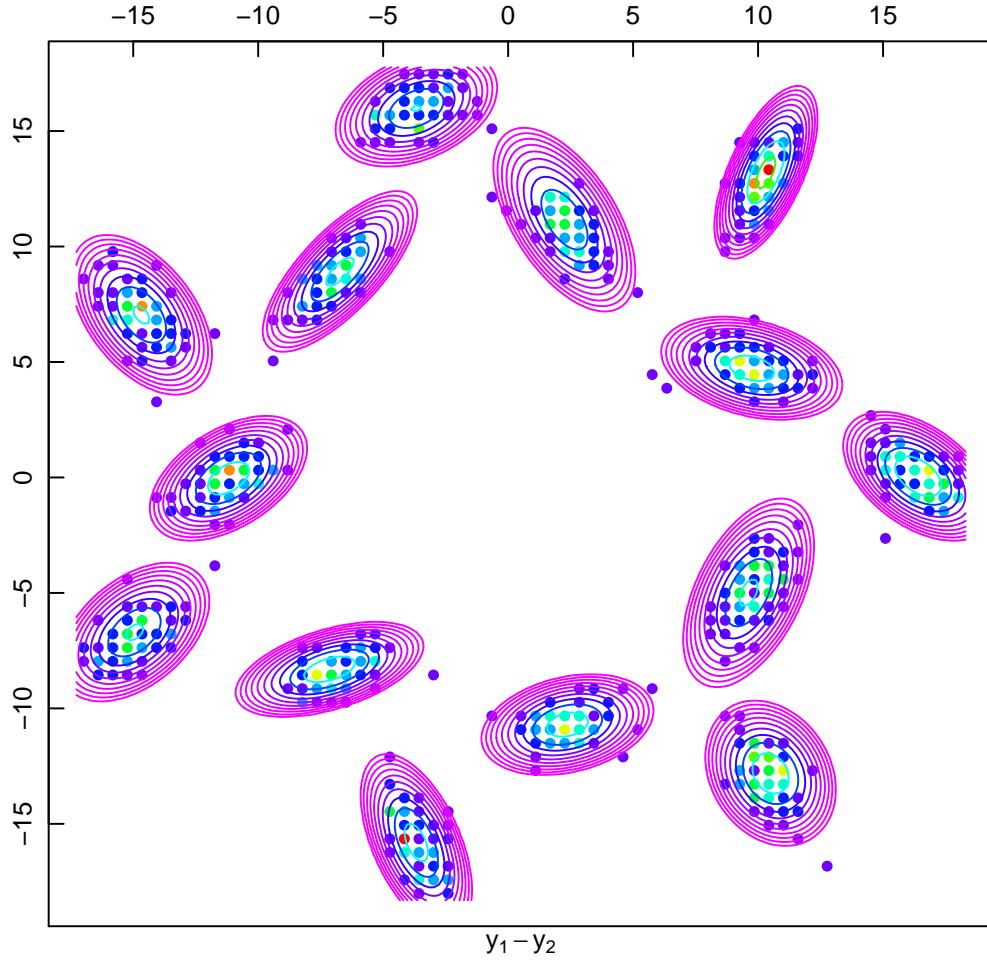


Figure 4: Dataset `wreath`. Empirical densities (coloured circles), predictive multivariate normal mixture density (coloured lines).

```
theta2.11 1.111 0.929 0.929 1.409
theta2.12 0.974 -0.780 -0.780 1.912
theta2.13 0.809 0.625 0.625 1.963
theta2.14 1.061 0.477 0.477 1.063
```

3.3.3 Plot method

3.3.4 Clustering

3.4 Multivariate normal ex4.1 dataset

A `ex4.1` dataset (Baudry et al., 2005; Fraley et al., 2016) consist of 600 two dimensional observations.

3.4.1 Finite mixture estimation

```
R> data("Baudry_et al_2010_JCGS_examples", package = "mclust")
R> n <- nrow(ex4.1)
R> K <- c(as.integer(1 + log2(sum(n))), as.integer(2 * sum(n)^0.5))
```

```
R> wreathclu <- RCLRMIX(model = "RCLRMVNORM", x = wreathest)
R> plot(wreathclu)
```

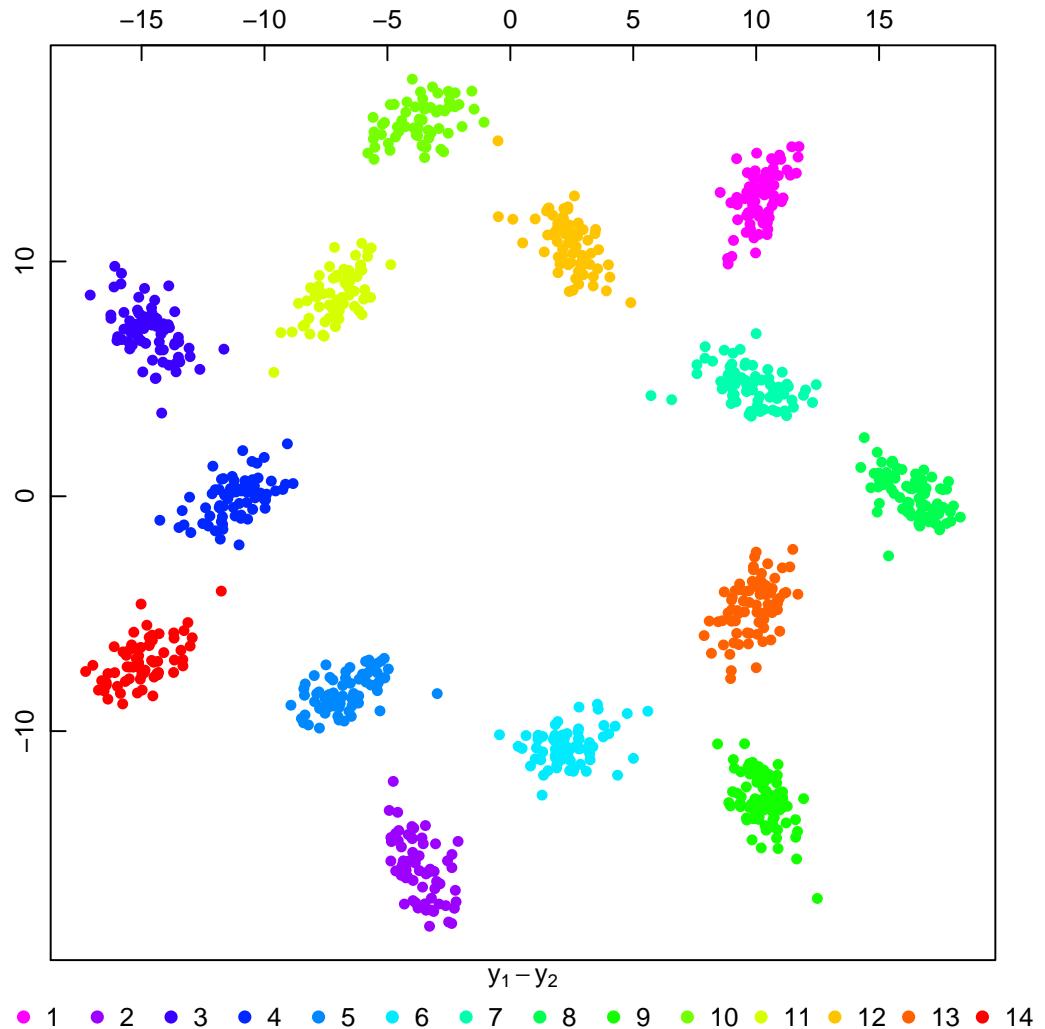
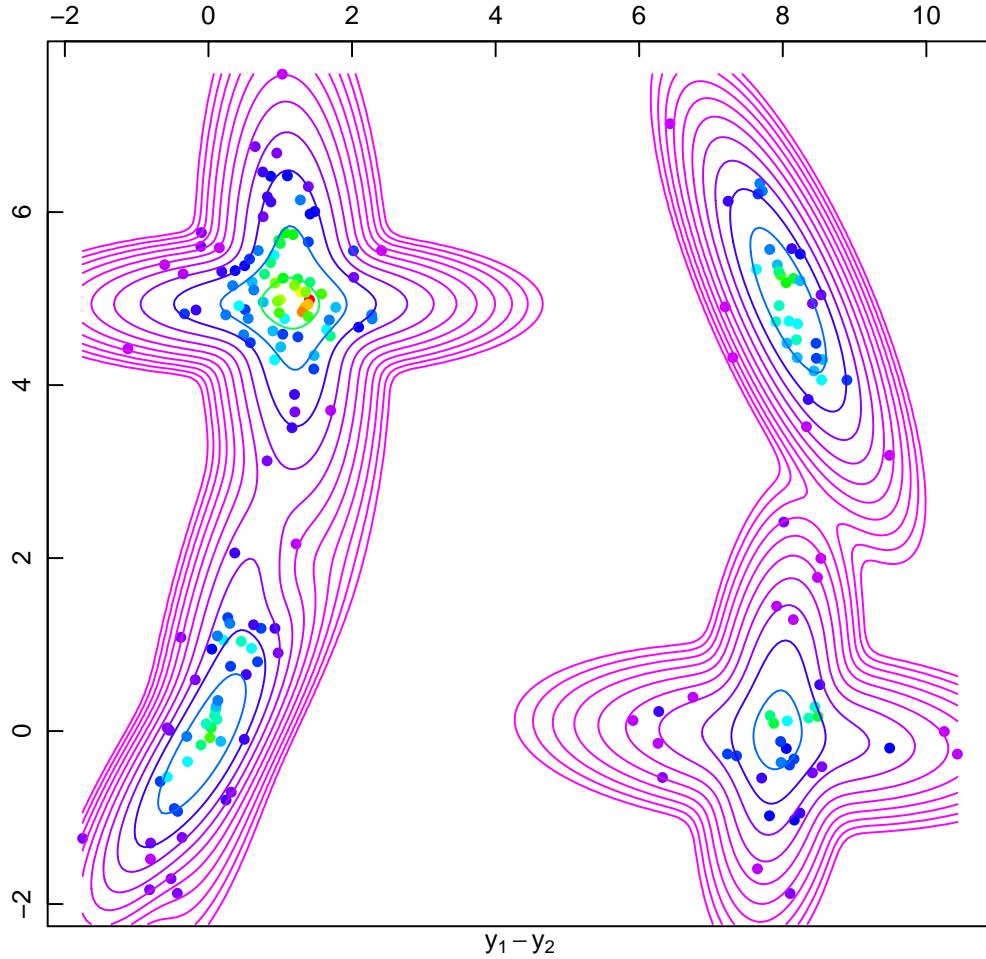


Figure 5: Dataset `wreath`. Predictive cluster membership (coloured circles).

```
R> plot(ex4.1est, pos = 1, what = c("dens"), nrow = 1, ncol = 1)
```



Dataset = dataset1, Preprocessing = Parzen window, Restraints = loose, $c_{\max} = 10$, $a_r = 0.1$, $c = 7$, $v = 29$, AIC = 4040, log L = -1979.

Figure 6: Dataset ex4.1. Empirical densities (coloured circles), predictive multivariate normal mixture density (coloured lines).

```
R> ex4.1est <- REBMIX(model = "REBMVNORM", Dataset = list(as.data.frame(ex4.1)),
+   Preprocessing = "Parzen window", cmax = 10, Criterion = "AIC",
+   pdf = rep("normal", ncol(ex4.1)), K = K[1]:K[2])
```

3.4.2 Summary method

```
R> summary(ex4.1est)
```

	Dataset	Preprocessing	Criterion	c	v/k	IC	logL	M
1	dataset1	Parzen window	AIC	7	29	4040	-1979	41

Maximum logL = -1979 at pos = 1.

3.4.3 Plot method

3.4.4 Clustering

```
R> ex4.1clu <- RCLRMIX(model = "RCLRMVNORM", x = ex4.1est)
R> plot(ex4.1clu)
```

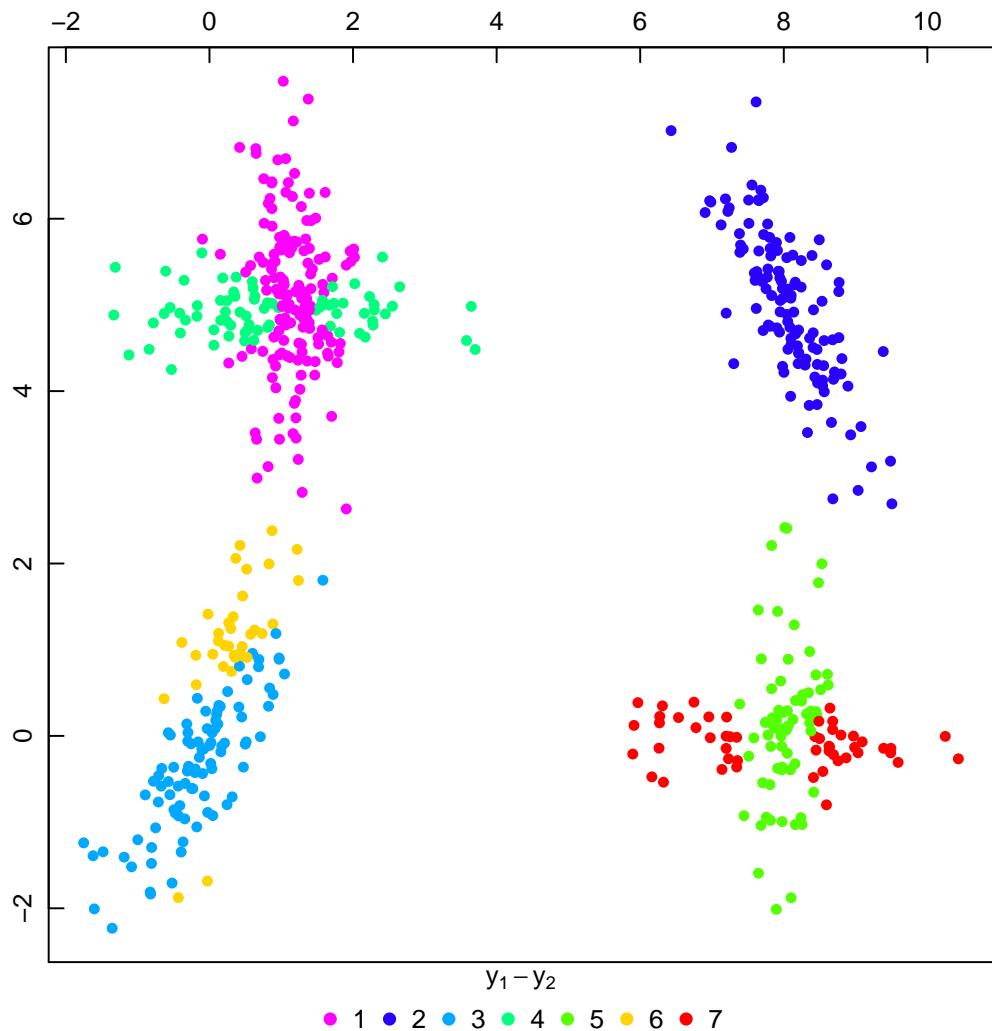


Figure 7: Dataset ex4.1. Predictive cluster membership (coloured circles).

3.5 Multivariate iris dataset

The well known set of iris data as collected originally by Anderson (1936) and first analysed by Fisher (1936) is considered here. It is available at Asuncion and Newman (2007) consisting of the measurements of the length and width of both sepals and petals of 50 plants for each of the three types of iris species setosa, versicolor and virginica. The iris dataset is loaded, split into three subsets for the three classes and the Class column is removed.

```
R> data("iris")
R> levels(iris[["Class"]])
[1] "iris-setosa"      "iris-versicolor" "iris-virginica"

R> iris_set <- subset(iris, subset = Class == "iris-setosa", select = c(-Class))
R> iris_ver <- subset(iris, subset = Class == "iris-versicolor",
+   select = c(-Class))
R> iris_vir <- subset(iris, subset = Class == "iris-virginica",
+   select = c(-Class))
```

The datasets are split into train (75%) and test (25%) datasets.

```
R> set.seed(5)
R> Prob <- 0.75
R> n_set <- nrow(iris_set)
R> s_set <- sample.int(n = n_set, size = as.integer(n_set * Prob))
R> iris_set_train <- iris_set[s_set, ]
R> iris_set_test <- iris_set[-s_set, ]
R> n_ver <- nrow(iris_ver)
R> s_ver <- sample.int(n = n_ver, size = as.integer(n_ver * Prob))
R> iris_ver_train <- iris_ver[s_ver, ]
R> iris_ver_test <- iris_ver[-s_ver, ]
R> n_vir <- nrow(iris_vir)
R> s_vir <- sample.int(n = n_vir, size = as.integer(n_vir * Prob))
R> iris_vir_train <- iris_vir[s_vir, ]
R> iris_vir_test <- iris_vir[-s_vir, ]
R> iris_test = rbind(iris_set_test, iris_ver_test, iris_vir_test)
```

Factor Z_t of true class membership is stored for the test datasets.

```
R> Zt <- factor(c(rep(0, nrow(iris_set_test)), rep(1, nrow(iris_ver_test)),
+   rep(2, nrow(iris_vir_test))))
```

3.5.1 Finite mixture estimation

```
R> n <- range(nrow(iris_set_train), nrow(iris_ver_train), nrow(iris_vir_train))
R> K <- c(as.integer(1 + log2(sum(n[1]))), as.integer(10 * log10(n[2])))
R> K <- c(floor(K[1]^(1/4)), ceiling(K[2]^(1/4)))
R> irisest <- REBMIX(model = "REBMVNORM", Dataset = list(iris_set_train = iris_set_train,
+   iris_ver_train = iris_ver_train, iris_vir_train = iris_vir_train),
+   Preprocessing = "Parzen window", cmax = 10, Criterion = "ICL-BIC",
+   pdf = rep("normal", 4), K = K[1]:K[2])
```

3.5.2 Classification

```
R> irisclla <- RCLSMIX(model = "RCLSMVNORM", x = list(irisest), Dataset = iris_test,
+   Zt = Zt)
```

3.5.3 Show and summary methods

```
R> iriscla  
  
An object of class "RCLSMVNORM"  
Slot "CM":  
  1  2  3  
1 13  0  0  
2  0 13  0  
3  0  1 12  
Slot "Error":  
[1] 0.0256  
Slot "Precision":  
[1] 1.000 1.000 0.923  
Slot "Sensitivity":  
[1] 1.000 0.929 1.000  
Slot "Specificity":  
[1] 1.000 1.040 0.963
```

```
R> summary(iriscla)
```

	Test	Predictive	Frequency
1	1	1	13
2	2	1	0
3	3	1	0
4	1	2	0
5	2	2	13
6	3	2	1
7	1	3	0
8	2	3	0
9	3	3	12

Error = 0.0256.

3.5.4 Plot method

3.6 Multivariate adult dataset

The **adult** dataset containing 48842 instances with 16 continuous, binary and discrete variables was extracted from the census bureau database Asuncion and Newman (2007). Extraction was done by Barry Becker from the 1994 census bureau database. The **adult** dataset is loaded, complete cases are extracted and levels are replaced with numbers.

```
R> data("adult")  
R> adult <- adult[complete.cases(adult), ]  
R> adult <- as.data.frame(data.matrix(adult))
```

The dataset is split into two train subsets for the two incomes and the **Type** and **Income** columns are removed.

```
R> trainle50k <- subset(adult, subset = (Type == 2) & (Income ==  
+     1), select = c(-Type, -Income))  
R> traingt50k <- subset(adult, subset = (Type == 2) & (Income ==  
+     2), select = c(-Type, -Income))  
R> trainall <- subset(adult, subset = Type == 2, select = c(-Type,  
+     -Income))  
R> train <- as.factor(subset(adult, subset = Type == 2, select = c(Income))[,  
+     1])
```

R> `plot(iriscla, nrow = 3, ncol = 2)`

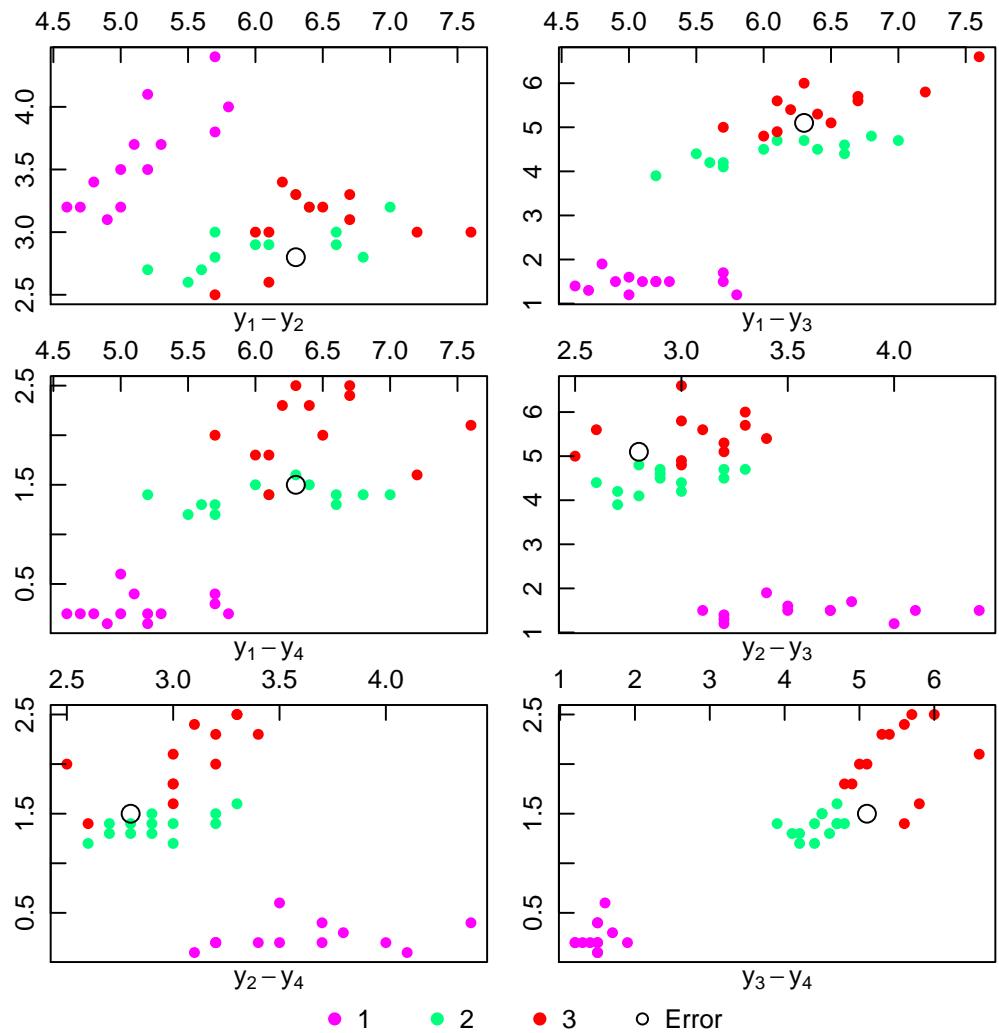


Figure 8: Dataset `iris`. Predictive class membership (coloured circles), error (large circles).

Two test datasets are extracted from the adult dataset and the Type and Income columns are removed.

```
R> testle50k <- subset(adult, subset = (Type == 1) & (Income ==  
+     1), select = c(-Type, -Income))  
R> testgt50k <- subset(adult, subset = (Type == 1) & (Income ==  
+     2), select = c(-Type, -Income))  
R> testall <- subset(adult, subset = Type == 1, select = c(-Type,  
+     -Income))  
R> test <- as.factor(subset(adult, subset = Type == 1, select = c(Income))[,  
+     1])
```

3.6.1 Finite mixture estimation

Variables are assumed to be independent and continuous or discrete depending on the number of distinct values `cmax` across the set of variables.

```
R> cmax <- unlist(lapply(apply(trainall, 2, unique), length))  
R> adulptest <- list(0)  
R> for (i in 1:14) {  
+     adulptest[[i]] <- REBMIX(Dataset = list(as.data.frame(trainle50k[  
+         i]), as.data.frame(traintg50k[, i])), Preprocessing = "histogram",  
+         cmax = if (cmax[i] > 120)  
+             12  
+         else cmax[i], Criterion = "BIC", pdf = if (cmax[i] >  
+             120)  
+                 "normal"  
+             else "Dirac", K = if (cmax[i] > 120)  
+                 13:43  
+             else 1)  
+ }
```

3.6.2 Best-first feature subset selection

```
R> c <- NULL  
R> rvs <- 1:14  
R> Error <- 1  
R> for (i in 1:14) {  
+     k <- NA  
+     for (j in rvs) {  
+         adultcla <- RCLSMIX(x = adulptest[c(c, j)], Dataset = as.data.frame(trainall[  
+             c(c, j)]), Zt = train)  
+         if (adultcla@Error < Error) {  
+             Error <- adultcla@Error  
+             k <- j  
+         }  
+     }  
+     if (is.na(k)) {  
+         break  
+     }  
+     else {  
+         c <- c(c, k)  
+         rvs <- rvs[-which(rvs == k)]  
+     }  
+ }  
R> Error
```

```
[1] 0.139
```

3.6.3 Classification

```
R> adultcla <- RCLSMIX(x = adulttest[c], Dataset = as.data.frame(testall[,  
+ c]), Zt = test)
```

3.6.4 Show and summary methods

```
R> adultcla
```

An object of class "RCLSMIX"

Slot "CM":

	1	2
1	10649	711
2	1397	2303

Slot "Error":

```
[1] 0.14
```

Slot "Precision":

```
[1] 0.937 0.622
```

Slot "Sensitivity":

```
[1] 0.884 0.764
```

Slot "Specificity":

```
[1] 1.228 0.943
```

```
R> summary(adultcla)
```

Test	Predictive Frequency
1	1 10649
2	2 1397
3	1 711
4	2 2303

Error = 0.14.

3.6.5 Plot method

4 Summary

The users of the `rebmix` package are kindly encouraged to inform the author about bugs and wishes.

References

- E. Anderson. The species problem in iris. *Annals of the Missouri Botanical Garden*, 23(3):457–509, 1936. doi: 10.2307/2394164.
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```
R> plot(adultcla, nrow = 5, ncol = 2)
```

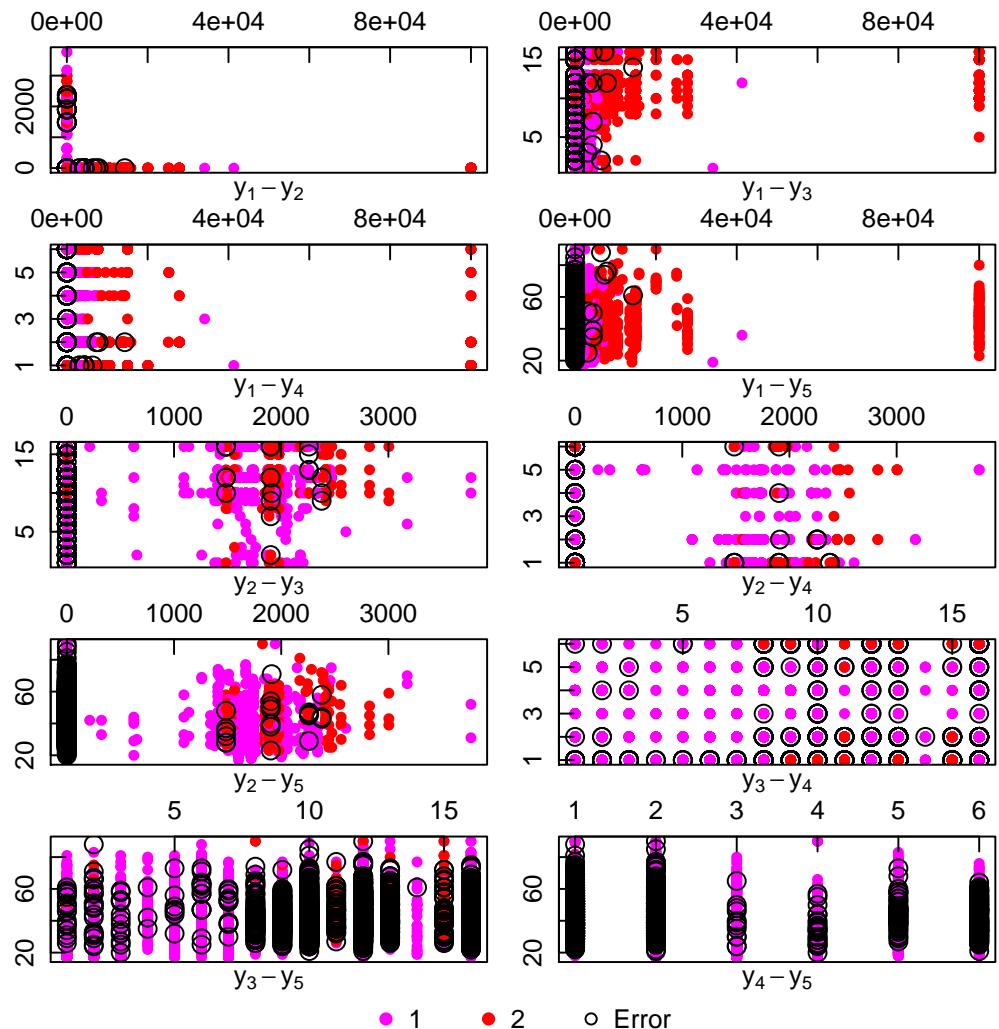


Figure 9: Dataset adult. Predictive class membership (coloured circles), error (large circles).

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