On the usage of the `geepack`

Søren Højsgaard and Ulrich Halekoh

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Contents

1 Introduction

This note contains a few extra examples. We illustrate the usage of a the `waves` argument and the `zcor` argument together with a fixed working correlation matrix for the `geeglm()` function.

2 Citing `geepack`

The primary reference for the `geepack` package is

> Halekoh, U., Højsgaard, S., Yan, J. (2006) *The R Package geepack for Generalized Estimating Equations (2006)* Journal of Statistical Software `https://www.jstatsoft.org/article/view/v015i02`

```
> library(geepack)
> citation("geepack")

To cite geepack in publications use:

  Højsgaard, S., Halekoh, U. & Yan J. (2006) The R Package geepack for
  Generalized Estimating Equations Journal of Statistical Software, 15,
  2, pp1--11

  Yan, J. & Fine, J.P. (2004) Estimating Equations for Association
  Structures Statistics in Medicine, 23, pp859--880.

  Yan, J (2002) geepack: Yet Another Package for Generalized Estimating
  Equations R-News, 2/3, pp12-14.

To see these entries in BibTeX format, use 'print(<citation>,
bibtex=TRUE)', 'toBibtex(.)', or set
'options(citation.bibtex.max=999)'.
```

If you use `geepack` in your own work, please do cite the above reference.

3 Simulating a dataset

To illustrate the usage of the `waves` argument and the `zcor` argument together with a fixed working correlation matrix for the `geeglm()` we simulate some data suitable for a regression model.

```
> library(geepack)
> timeorder <- rep(1:5, 6)
> tvar      <- timeorder + rnorm(length(timeorder))
> idvar <- rep(1:6, each=5)
> uuu   <- rep(rnorm(6), each=5)
> yvar  <- 1 + 2*tvar + uuu + rnorm(length(tvar))
> simdat <- data.frame(idvar, timeorder, tvar, yvar)
> head(simdat,12)

   idvar timeorder       tvar       yvar
1      1         1 0.31623517  1.7852996
2      1         2 0.22954452  3.3669341
3      1         3 2.33631576  8.3905173
4      1         4 3.13311147  9.9633033
5      1         5 6.74261004 15.5395544
6      2         1 1.46351662  4.1724731
7      2         2 1.78414567  3.2113352
8      2         3 2.78216593  6.2039885
9      2         4 4.82102005 10.7159724
10     2         5 6.63738201 14.0233425
11     3         1 1.74970012  4.5376941
12     3         2 0.02002667  0.3597233
```

Notice that clusters of data appear together in `simdat` and that observations are ordered (according to `timeorder`) within clusters.

We can fit a model with an AR(1) error structure as

```
> mod1 <- geeglm(yvar~tvar, id=idvar, data=simdat, corstr="ar1")
> mod1

Call:
geeglm(formula = yvar ~ tvar, data = simdat, id = idvar, corstr = "ar1")

Coefficients:
(Intercept)        tvar
   1.556930    2.019076

Degrees of Freedom: 30 Total (i.e. Null);  28 Residual

Scale Link:                   identity
Estimated Scale Parameters:  [1] 2.220208

Correlation:  Structure = ar1    Link = identity
Estimated Correlation Parameters:
   alpha
0.832623

Number of clusters:   6   Maximum cluster size: 5
```

This works because observations are ordered according to time within each subject in the dataset.

4 Using the `waves` argument

If observatios were not ordered according to cluster and time within cluster we would get the wrong result:

```
> set.seed(123)
> ## library(doBy)
> simdatPerm <- simdat[sample(nrow(simdat)),]
> ## simdatPerm <- orderBy(~idvar, simdatPerm)
> simdatPerm <- simdatPerm[order(simdatPerm$idvar),]
> head(simdatPerm)

   idvar timeorder      tvar      yvar
3      1         3 2.3363158  8.390517
5      1         5 6.7426100 15.539554
4      1         4 3.1331115  9.963303
1      1         1 0.3162352  1.785300
2      1         2 0.2295445  3.366934
10     2         5 6.6373820 14.023342
```

Notice that in `simdatPerm` data is ordered according to subject but the time ordering within subject is random.

Fitting the model as before gives

```
> mod2 <- geeglm(yvar~tvar, id=idvar, data=simdatPerm, corstr="ar1")
> mod2

Call:
geeglm(formula = yvar ~ tvar, data = simdatPerm, id = idvar,
    corstr = "ar1")

Coefficients:
(Intercept)        tvar
   1.440798    2.085604

Degrees of Freedom: 30 Total (i.e. Null);  28 Residual

Scale Link:                   identity
Estimated Scale Parameters:  [1] 2.242069

Correlation:  Structure = ar1    Link = identity
Estimated Correlation Parameters:
   alpha
0.838116

Number of clusters:   6   Maximum cluster size: 5
```

Likewise if clusters do not appear contigously in data we also get the wrong result (the clusters are not recognized):

```
> ## simdatPerm2 <- orderBy(~timeorder, data=simdat)
> simdatPerm2 <- simdat[order(simdat$timeorder),]
> geeglm(yvar~tvar, id=idvar, data=simdatPerm2, corstr="ar1")

Call:
geeglm(formula = yvar ~ tvar, data = simdatPerm2, id = idvar,
    corstr = "ar1")

Coefficients:
(Intercept)        tvar
   1.327591    2.063154

Degrees of Freedom: 30 Total (i.e. Null);  28 Residual

Scale Link:                   identity
Estimated Scale Parameters:  [1] 2.205582

Correlation:  Structure = ar1    Link = identity
Estimated Correlation Parameters:
alpha
    0

Number of clusters:   30   Maximum cluster size: 1
```

To obtain the right result we must give the `waves` argument:

```
> wav <- simdatPerm$timeorder
> wav

 [1] 3 5 4 1 2 5 4 3 2 1 5 4 1 3 2 4 3 5 2 1 2 4 5 3 1 3 2 1 5 4

> mod3 <- geeglm(yvar~tvar, id=idvar, data=simdatPerm, corstr="ar1", waves=wav)
> mod3

Call:
geeglm(formula = yvar ~ tvar, data = simdatPerm, id = idvar,
    waves = wav, corstr = "ar1")

Coefficients:
(Intercept)        tvar
   1.556930    2.019076

Degrees of Freedom: 30 Total (i.e. Null);  28 Residual

Scale Link:                   identity
Estimated Scale Parameters:  [1] 2.220208

Correlation:  Structure = ar1    Link = identity
Estimated Correlation Parameters:
   alpha
0.832623

Number of clusters:   6   Maximum cluster size: 5
```

5 Using a fixed correlation matrix and the `zcor` argument

Suppose we want to use a fixed working correlation matrix:

```
> cor.fixed <- matrix(c(1    , 0.5  , 0.25,  0.125, 0.125,
+                       0.5  , 1    , 0.25,  0.125, 0.125,
+                       0.25 , 0.25 , 1   ,  0.5  , 0.125,
+                       0.125, 0.125, 0.5  , 1    , 0.125,
+                       0.125, 0.125, 0.125, 0.125, 1     ), 5, 5)
> cor.fixed

      [,1]  [,2]  [,3]  [,4]  [,5]
[1,] 1.000 0.500 0.250 0.125 0.125
[2,] 0.500 1.000 0.250 0.125 0.125
[3,] 0.250 0.250 1.000 0.500 0.125
[4,] 0.125 0.125 0.500 1.000 0.125
[5,] 0.125 0.125 0.125 0.125 1.000
```

Such a working correlation matrix has to be passed to `geeglm()` as a vector in the `zcor` argument. This vector can be created using the `fixed2Zcor()` function:

```
> zcor <- fixed2Zcor(cor.fixed, id=simdatPerm$idvar, waves=simdatPerm$timeorder)
> zcor

 [1] 0.125 0.500 0.250 0.250 0.125 0.125 0.125 0.125 0.125 0.500 0.125 0.125
[13] 0.125 0.125 0.500 0.125 0.125 0.250 0.250 0.500 0.125 0.125 0.125 0.125
[25] 0.125 0.500 0.125 0.250 0.500 0.250 0.500 0.125 0.125 0.125 0.125 0.250
[37] 0.250 0.125 0.125 0.500 0.125 0.125 0.250 0.500 0.125 0.500 0.125 0.125
[49] 0.125 0.250 0.250 0.250 0.125 0.500 0.500 0.125 0.125 0.125 0.125 0.125
```

Notice that `zcor` contains correlations between measurements within the same cluster. Hence if a cluster contains only one observation, then there will be generated no entry in `zcor` for that cluster. Now we can fit the model with:

```
> mod4 <- geeglm(yvar~tvar, id=idvar, data=simdatPerm, corstr="fixed", zcor=zcor)
> mod4

Call:
geeglm(formula = yvar ~ tvar, data = simdatPerm, id = idvar,
    zcor = zcor, corstr = "fixed")

Coefficients:
(Intercept)        tvar
   1.323688    2.064315

Degrees of Freedom: 30 Total (i.e. Null);  28 Residual

Scale Link:                   identity
Estimated Scale Parameters:  [1] 2.205587

Correlation:  Structure = fixed    Link = identity
Estimated Correlation Parameters:
alpha:1
      1

Number of clusters:   6   Maximum cluster size: 5
```

6 When do GEE's work best?

GEEs work best when you have relatively many relativly small clusters in your data.