

replication.SDA(symbolicDA)

Modification of replication analysis for cluster validation of symbolic data

Formally, replicating clusters proceeds as follows (see Breckenridge [2000], 262-263; Milligan [1996], 368-369; Gordon [1999], 184):

1. The data are randomly divided into two samples: sample A (primary set) and sample B (replication set). Data must exist on the same set of variables in both samples.

2. Sample A is clustered into u clusters $A = \{A_1, \dots, A_u\}$ via optimization method: SClust, DClust, pam or hierarchical method: single, complete, average, mcquitty, median, centroid, Ward, diana (see e.g. Bock, Diday [2000]; Diday, Noirhomme-Fraiture [2008]). Once clusters have been identified, the medoids of u clusters are selected.

3. Sample B is clustered, using the same clustering procedure, into u clusters $B = \{B_1, \dots, B_u\}$.

4. The distances between sample B objects and the medoids of sample A are determined (see e.g. Bock, Diday [2000]; Diday, Noirhomme-Fraiture [2008]). Each element of sample B is assigned to the nearest medoid determined in step 2 (this provides a partition of sample B into no more than u clusters). This produces a clustering of sample B based on characteristics of sample A : $B^* = \{B_1^*, \dots, B_u^*\}$.

5. The steps 1-4 are repeated S times (S – the number of simulations).

6. A measure of agreement (average value of adjusted Rand index) between two clusterings B and B^* are computed for S simulations. The level of agreement between the two partitions reflects the stability of the clustering in the data. Adjusted Rand index takes values of $(-\infty, 1]$ and its value close to 1 means relatively stable division of objects set into u clusters.

References

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